

## Projection of Life Expectancy at Birth for the Population of Urban Area in Bangladesh

*Background: Life expectancy at birth (LE) reflects the overall mortality of a population and it is also used as one of the indicators of the health status of population. Objective: The main purpose of this study is to project LE for the population of male, female and both sexes of urban region in Bangladesh by using polynomial model. Data and Methodology: For this purpose, the data is obtained from Statistical Year Book (SYB) of Bangladesh of 2012. Quasi Newton Method is used to build up these models using the Statistical software STATISTICA. Furthermore, t-test statistics, F-test statistics and cross validity prediction power (CVPP) are applied to identify the correctness of these model. Results: It is found that LE for the population of urban region of Bangladesh follow simple linear regression model. Based on t-stats, coefficient of determination, shrinkage coefficients and F-stats these models are seemed to be well fitted. So, these models can be used for better prediction. Then, these LE are projected during 2012-2051 using the fitted time trend models. It is observed that the LE for the population of male, female and both sexes of urban region of Bangladesh in 2051 are 75, 84.1 and 78 years respectively. Conclusion: Urban population of Bangladesh are going to be aged population dramatically. Proper planning for the allocation of public and private resources may be taken for the better lifestyle of urban population.*

**Keywords:** *Life expectancy at birth (LE), Polynomial model, t-test statistics, F-test statistics, Cross validity prediction power (CVPP), Bangladesh*

### Introduction

Life expectancy is demarcated as the average number of supplementary years that a person of a specific age group will live, if the current age-specific mortality schedules remain constant over the course of the individual's lifetime (Chiang, 1968). Life expectancy is an indirect measure of mortality and it is also the main indicator of health status of a society or a country or a region. On the other hand, education and health are the leading sectors for socio-economic development for the developing countries like Bangladesh. Life expectancies in urban and rural areas for the population of male, female and both sexes from 1994 to 2011 show the shortest life expectancy of those living in rural area than that of urban areas (BBS, 2014). Life expectancy at birth (LE) in Bangladesh is poor in international comparisons with median of LE for male and female are 70 and 76 years respectively in 2011 (WHO, 2013). Life expectancy is not the measure of the aged population, but it shows the present situation of socio-economic development of a country. Moreover, it is found that LE of Bangladesh is increasing with the increase of time (BBS, 2013). Like many other nations, in Bangladesh female live lengthier than male and this gender difference in the LE has been increasing with passing of time. The longer LE of female population does not necessarily provide that the female are healthier

1 than male. Studies on self-reported health status measure specify higher  
 2 prevalence of functional restrictions and poor health among female (Parahyba  
 3 et al., 2005; Lima et al., 2009; Zunzunegui et al., 2009 and Szwarcwald et al.,  
 4 2011), suggesting that the additional years cannot essentially be lived in hale  
 5 and hearty life. LE is increasing every year that means aged population is  
 6 increasing in Bangladesh. So, especially government and policy makers should  
 7 have clear concept about the number of aged population to ensure them with  
 8 healthy environment. For this, correct information of LE in the future years is  
 9 needed to take several steps for development of education, health, environment  
 10 and others socioeconomic related sectors of Bangladesh. For this reason,  
 11 mathematical model is selected to observe the trend of LE for the population of  
 12 urban areas in Bangladesh. To do so, polynomial model has been chosen in this  
 13 study. It is mentioned here that polynomial model was applied in a number of  
 14 studies like as (Islam, 2004, 2005a; 2005b; 2007a and 2011; Islam et al., 2004  
 15 and 2014; Islam and Hossain, 2014a and 2014b). Therefore, the fundamental  
 16 aims of this study are to construct some models to LE for the population of  
 17 male, female and both sexes of urban region in Bangladesh and then to project  
 18 LE for them employing these fitted models for the period 2012-2051.

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### 21 **Source of Data**

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23 A data on LE for the population of men, women and both sexes of urban  
 24 region in Bangladesh during 2002-2011 have been obtained from SYB of  
 25 Bangladesh of 2012 (BBS, 2013) which are shown in Table 1. To fulfill the  
 26 above objectives, these LE data are used in this study.

27

28 **Table 1.** *Observed LE for Male, Female and Both Sexes of the Population of*  
 29 *Urban Area in Bangladesh during 2002-2011*

| Year | Male | Female | Both Sexes |
|------|------|--------|------------|
| 2002 | 67.0 | 67.3   | 67.2       |
| 2003 | 67.3 | 67.9   | 67.6       |
| 2004 | 67.5 | 68.1   | 67.8       |
| 2005 | 67.6 | 68.1   | 67.9       |
| 2006 | 67.7 | 68.7   | 68.1       |
| 2007 | 67.7 | 68.7   | 68.1       |
| 2008 | 67.9 | 68.8   | 68.3       |
| 2009 | 68.2 | 69.2   | 68.7       |
| 2010 | 68.3 | 69.5   | 68.9       |
| 2011 | 68.9 | 71.1   | 69.9       |

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**Source:** BBS (2013) Statistical Year Book of Bangladesh 2012.

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1 **Methods**

2

3 *Data Smoothing*

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5 In this paper, it is found that there are some kinds of unexpected  
6 distortions in the data set if LE is dotted on a graph paper. For that reason, an  
7 adjustment is imperative and needed to abate these unexpected distortions  
8 before going to construct model to these data. In this situation, the data of LE  
9 for the population of men, women and both sexes of are smoothened by the  
10 Package Minitab Release 12.1 by smoothing technique named “4253H, twice”  
11 (Velleman, 1980). After that, these smoothed data are taken to build models  
12 and these smoothed data are presented in the Table 2.

13

14 **Table 3.** *Smoothed and Predicted LE for Male, Female and Both Sexes of the*  
15 *Population of Urban Area in Bangladesh during 2002-2011*

| Year | Male     |           | Female   |           | Both Sexes |           |
|------|----------|-----------|----------|-----------|------------|-----------|
|      | Smoothed | Predicted | Smoothed | Predicted | Smoothed   | Predicted |
| 2002 | 67.0     | 67.0      | 67.4     | 67.3      | 67.2       | 67.2      |
| 2003 | 67.3     | 67.2      | 67.8     | 67.6      | 67.6       | 67.4      |
| 2004 | 67.5     | 67.3      | 68.1     | 68.0      | 67.8       | 67.7      |
| 2005 | 67.6     | 67.5      | 68.3     | 68.3      | 67.9       | 67.9      |
| 2006 | 67.7     | 67.6      | 68.5     | 68.7      | 68.0       | 68.1      |
| 2007 | 67.7     | 67.8      | 68.7     | 69.0      | 68.1       | 68.3      |
| 2008 | 67.9     | 68.0      | 69.1     | 69.3      | 68.3       | 68.5      |
| 2009 | 68.1     | 68.1      | 69.5     | 69.7      | 68.6       | 68.8      |
| 2010 | 68.4     | 68.3      | 69.9     | 70.0      | 69.0       | 69.0      |
| 2011 | 68.7     | 68.5      | 71.0     | 70.4      | 69.6       | 69.2      |

16

17 *Model Building*

18

19 The polynomial model is chosen to fit model (using the scattered plot of  
20 Fig.1-Fig.3) to LE for the population of men, women and both sexes in urban  
21 region of Bangladesh. Therefore, the configuration of n degree polynomial  
22 model is addressed by

23

$$24 \quad y_t = a_0 + \sum_{i=1}^n a_i t^i + u$$

25

26 where, t represents time (years);  $y_t$  represents LE; the coefficient of  $t^i$  is  $a_i$ ,  $a_0$  is  
27 the constant term and u is the error term of the model. In this case, n is chosen  
28 so that the error sum of square is minimum. Moreover, it is noted that actually  
29 disturbance term (u) of the model is normally as well as independently  
30 distributed with mean zero and constant variance, that is,  $u_i \sim \text{NID}(0, \sigma^2)$   
31 (Gujarati, 1998). In this case, it is found that if  $n=1$ , i. e., the polynomial model  
32 of degree one becomes simple linear regression model fitted to these data sets.

1 It is noted that these models are built using the Statistical software  
2 STATISTICA.

### 3 4 *Model Validation Procedure*

5  
6 To verify how a large amount of these models on LE are stable, the cross  
7 validity prediction power (CVPP),  $\rho_{cv}^2$ , is used for the urban area of  
8 Bangladesh. Here

$$9 \quad \rho_{cv}^2 = 1 - \frac{(n-1)(n-2)(n+1)}{n(n-k-1)(n-k-2)}(1-R^2); \text{ where, } n \text{ indicates the}$$

10 number of cases, k specifies the number of predictors for the model and the  
11 cross validated R denotes the correlation between observed and predicted  
12 values of the response variable (Stevens, 1996). The positive value of ( $\rho_{cv}^2 - R^2$ )  
13 mentions the shrinkage coefficient of the model; where  $\rho_{cv}^2$  is CVPP and  $R^2$  is  
14 the coefficient of determination of the model as well as the stability of  $R^2$  of  
15 the model is (1-shrinkage). The results on model fittings and estimated CVPP  
16 are presented in Table 3. A number of studies have been used this technique as  
17 validation (Islam, 2006a; 2006b; 2006c; 2007b; 2007c; 2008; 2012a; 2012b;  
18 2013; Islam & Hossain, 2013a; 2013b; Hossain & Islam, 2013; Islam et al.,  
19 2013; Islam and Hoque, 2015).

### 20 21 *F-test statistics*

22  
23 The F-test is employed to corroborate the measurement of overall  
24 significance of the model. The mathematical shape for F-test is specified under:

$$26 \quad F = \frac{R^2 / (k-1)}{(1-R^2) / (n-k)}$$

27  
28 where k represents the number of parameters of the model, n is the number of  
29 cases and  $R^2$  is the coefficient of determination of the fitted model (Gujarati,  
30 1998). These results are exposed in Table 4.

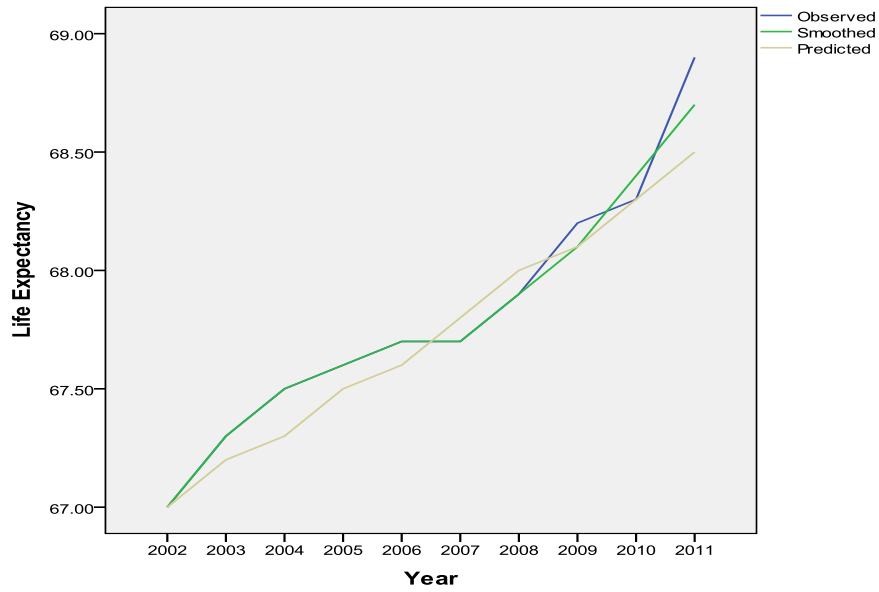
### 31 32 33 **Results**

34  
35 Table 1 and Table 2 represent the observed, smoothed and predicted LE  
36 for the population of men, women and both sexes of urban area in Bangladesh  
37 during 2002-2011. To see the level and trend of observed LE for the  
38 population, the data have been presented in graph paper shown in Fig. 4. It is  
39 investigated that the trend of LE for the population of men, women and both

1 sexes are showing upward. It is also seen that LE for female is higher than  
 2 male during 2002-2011. Observed, smoothed and predicted LE for the  
 3 population of men, women and both sexes during 2002-2011 are plotted in the  
 4 Fig.1 to Fig.3 respectively.

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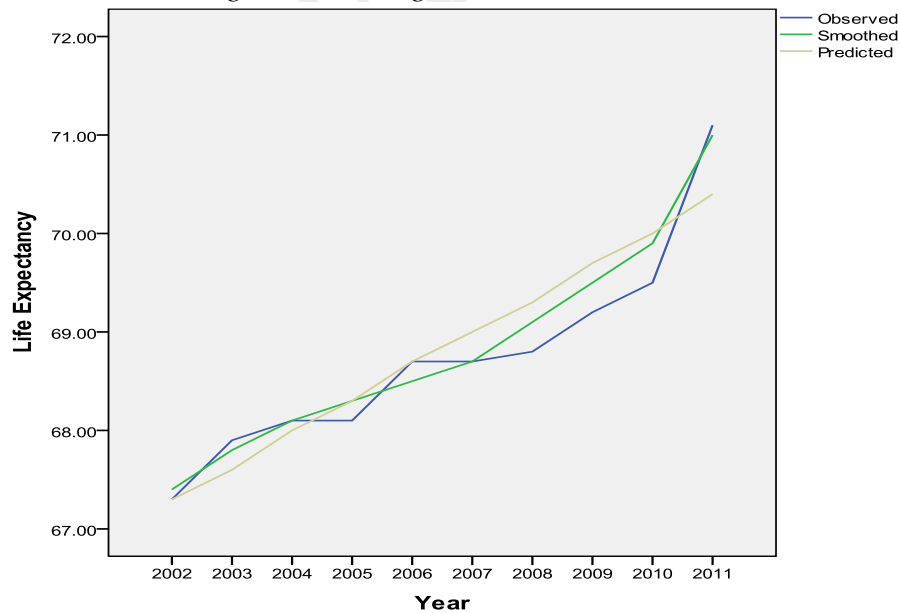
6 **Figure 1.** *Observed, Smoothed and Predicted LE for Male Population of*  
 7 *Urban Area in Bangladesh During 2002-2011. X: Years and Y: LE*



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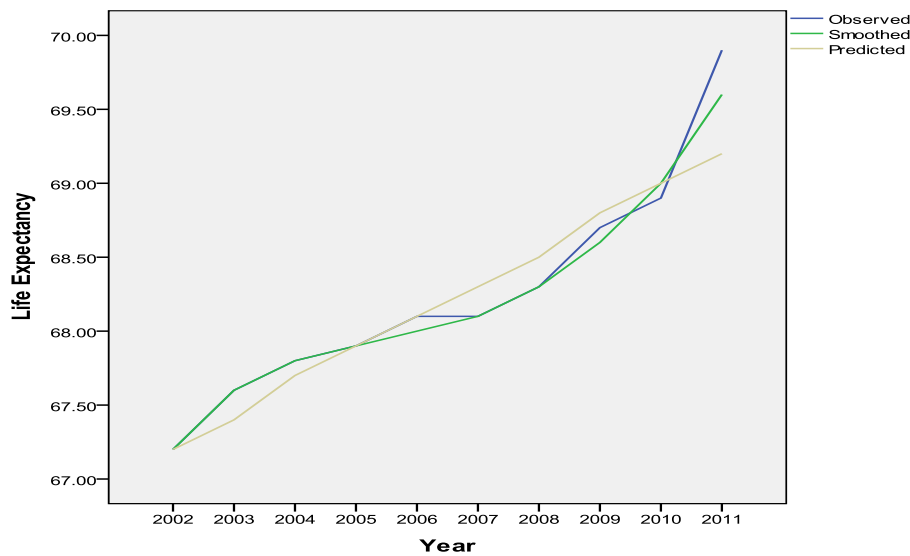
10 **Figure 2.** *Observed, Smoothed and Predicted LE for Female Population of*  
 11 *Urban Area in Bangladesh During 2002-2011. X: Years and Y: LE*



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1 **Figure 3.** *Observed, Smoothed and Predicted LE for Both Sexes of the*  
 2 *Population of Urban Area in Bangladesh During 2002-2011. X: Years and Y:*  
 3 *LE*



4  
 5 The model, that is, two parameters linear regression model is constructed  
 6 to LE for the population of male, female and both sexes of urban area in  
 7 Bangladesh and the constructed models are as follows:

8  
 9 
$$y_t = -259.330 + 0.163t \text{ for male} \quad (1)$$

10 t-stat (-9.7387) (12.2845)

11 P-value (0.0000) (0.0000)

12 
$$y_t = -620.676 + 0.344t \text{ for female} \quad (2)$$

13 t-stat (-9.6447) (10.7143)

14 P-value (0.0000) (0.0000)

15 
$$y_t = -378.084 + 0.222t \text{ for both sexes} \quad (3)$$

16 t-stat (-8.212) (9.693)

17 P-value (0.0000) (0.0000)

18

19 The enumerated CVPP,  $\rho_{cv}^2$  related to their  $R^2$  are demonstrated in Table 3.

20 From the table it is observed that the constructed models are highly cross-  
 21 validated and their shrinkages coefficients are very lowest. In the table, it is  
 22 found that the constructed models (1) – (3) are stable more than 92%, 90% and  
 23 91% respectively. Moreover, all the parameters of the constructed models (1) –  
 24 (3) are significant explaining large proportion of variance. The stabilities of  $R^2$   
 25 of these constructed models are more than 97%.

26

27

1 **Table 3.** *Information on Model Fittings and Estimated CVPP of the Predicted*  
 2 *Equations*

| Models     | N  | k | $R^2$   | $\rho_{cv}^2$ | Shrinkage  | Variance explained (%) |
|------------|----|---|---------|---------------|------------|------------------------|
| Equation 1 | 10 | 1 | 0.94966 | 0.928805      | 0.02085514 | 94.966                 |
| Equation 2 | 10 | 1 | 0.93485 | 0.907859      | 0.02699071 | 93.485                 |
| Equation 3 | 10 | 1 | 0.92154 | 0.889035      | 0.032505   | 92.15                  |

3  
 4 From these statistics of Table 4, it is also decided that all these fitted  
 5 models are highly significant. For this reason, the fits of all these models are  
 6 good. Then, the projected values of LE are estimated by applying these  
 7 constructed regression models that are exposed in Table 5. After plotting these  
 8 LE of men, women and both sexes of the population of urban area during  
 9 2012-2051 in the Fig.4, it shows an upward trend due to time like the trend  
 10 during 2002-2011. These projections of LE give an idea regarding the future  
 11 size of the oldest population in Bangladesh.

12  
 13 **Table 4.** *Information of Calculated and Tabulated Values of F-statistics of the*  
 14 *Predicted Equations*

| Models     | n  | K | Cal. F | Tab.F (at 1% level)  |
|------------|----|---|--------|----------------------|
| Equation 1 | 10 | 2 | 150.92 | 11.3 with (1,8) d.f. |
| Equation 2 | 10 | 2 | 114.79 | 11.3 with (1,8) d.f. |
| Equation 2 | 10 | 2 | 93.96  | 11.3 with (1,8) d.f. |

15  
 16 **Table 5.** *Projected LE for Male, Female and Both Sexes of the Population of*  
 17 *Urban Area in Bangladesh during 2012-2051*

| Year | Male | Female | Both Sexes |
|------|------|--------|------------|
| 2012 | 68.6 | 70.7   | 69.4       |
| 2013 | 68.8 | 71.1   | 69.6       |
| 2014 | 69.0 | 71.4   | 69.9       |
| 2015 | 69.1 | 71.8   | 70.1       |
| 2016 | 69.3 | 72.1   | 70.3       |
| 2017 | 69.4 | 72.4   | 70.5       |
| 2018 | 69.6 | 72.8   | 70.7       |
| 2019 | 69.8 | 73.1   | 71.0       |
| 2020 | 69.9 | 73.5   | 71.2       |
| 2021 | 70.1 | 73.8   | 71.4       |
| 2022 | 70.3 | 74.2   | 71.6       |
| 2023 | 70.4 | 74.5   | 71.8       |
| 2024 | 70.6 | 74.8   | 72.1       |
| 2025 | 70.7 | 75.2   | 72.3       |
| 2026 | 70.9 | 75.5   | 72.5       |
| 2027 | 71.1 | 75.9   | 72.7       |
| 2028 | 71.2 | 76.2   | 72.9       |

|      |      |      |      |
|------|------|------|------|
| 2029 | 71.4 | 76.6 | 73.2 |
| 2030 | 71.6 | 76.9 | 73.4 |
| 2031 | 71.7 | 77.2 | 73.6 |
| 2032 | 71.9 | 77.6 | 73.8 |
| 2033 | 72.0 | 77.9 | 74.0 |
| 2034 | 72.2 | 78.3 | 74.3 |
| 2035 | 72.4 | 78.6 | 74.5 |
| 2036 | 72.5 | 79.0 | 74.7 |
| 2037 | 72.7 | 79.3 | 74.9 |
| 2038 | 72.9 | 79.7 | 75.1 |
| 2039 | 73.0 | 80.0 | 75.4 |
| 2040 | 73.2 | 80.3 | 75.6 |
| 2041 | 73.4 | 80.7 | 75.8 |
| 2042 | 73.5 | 81.0 | 76.0 |
| 2043 | 73.7 | 81.4 | 76.2 |
| 2044 | 73.8 | 81.7 | 76.5 |
| 2045 | 74.0 | 82.1 | 76.7 |
| 2046 | 74.2 | 82.4 | 76.9 |
| 2047 | 74.3 | 82.7 | 77.1 |
| 2048 | 74.5 | 83.1 | 77.3 |
| 2049 | 74.7 | 83.4 | 77.6 |
| 2050 | 74.8 | 83.8 | 77.8 |
| 2051 | 75.0 | 84.1 | 78.0 |

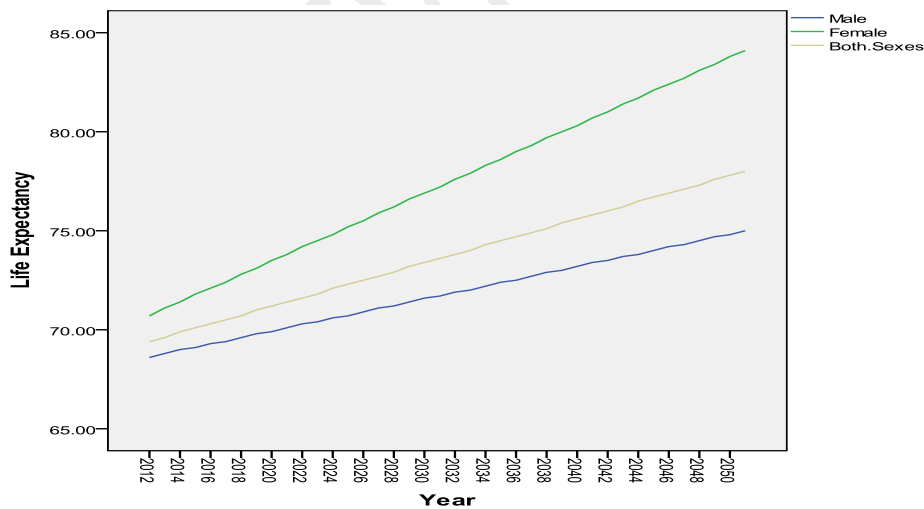
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**Figure 4.** Projected LE for Male, Female and Both Sexes of the Population of Urban Area in Bangladesh during 2012-2051. X: Years (Time) and Y: Projected LE



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## Discussion

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In the current study, the core objective was to project the LE of the urban populations of Bangladesh by sex. The simple linear regression model was employed as a method of projecting the LE. The projections were accomplished



1 up to the year 2051. The results revealed that the LE of the urban populations  
2 of Bangladesh by sex increase in accordance with time and female tend to live  
3 longer than male and it clearly exhibited the differences in LE between male  
4 and female. These findings conform to the study of Malaysian population (Is-  
5 lam et al., 2017). In this study, actually the LE was treated as the average num-  
6 ber of years of a person who can expect to live provided existing mortality pat-  
7 terns. The LE is treated as the most commonly used measurement of health sta-  
8 tus of population as well as, in fact, mortality. Nonetheless, LE should be fa-  
9 miliar as a measure of length of life rather than quality of life, on the contrary,  
10 it does not count the full burden of illness and disability.

11 In 2002, the LE in the urban populations of Bangladesh was 67.2 (male,  
12 67; female, 67.3) years (BBS, 2013), on the other hand, by 2051, it would be  
13 increased as 78 (male, 75; female, 84.1) years (projected). The long life can be  
14 attributed by a number of various types of factors together with rising living  
15 standards, enhanced lifestyle and improved quality education, as well as greater  
16 access to quality as well as available health services which are significantly  
17 increased LE in Bangladesh, especially in the urban area of Bangladesh. There-  
18 fore, the demographic and socioeconomic changes, and availability of health  
19 facilities persuade LE (Mondal and Shitan, 2013, 2014; Mondal et al, 2015). In  
20 Bangladesh, the expansion of population and the demographic transition since  
21 the 1971 were accompanied by major socioeconomic development. LE is af-  
22 fected by different factors such as socioeconomic status, social factors, genetic  
23 factors and environmental factors like income, education, the quality of the  
24 health system, health behaviors such as tobacco and alcohol consumption, poor  
25 nutrition, overcrowded housing, lack of clean drinking water, adequate sanita-  
26 tion, lack of exercise.

27 After the long years of socioeconomic development, Bangladesh had  
28 transformed into middle income country. accordingly, the socioeconomic de-  
29 velopment determines the improvements in social sectors and increases LE.  
30 Increases in LE have also been attributed by the substantial improvements in  
31 sanitation and the availability as well as easy access to clean drinking water  
32 (Mondal and Shitan, 2015). The sanitation system in Bangladesh has been im-  
33 proving radically which is imperatively as well as significantly high as the de-  
34 veloping nations. An increase in LE was driven mainly by the enhancement in  
35 sanitation in the time of the nineteenth and early twentieth century's (Oeppen  
36 and Vaupel, 2002). Environmental quality is a very important factor affecting  
37 health and morbidity: air and water pollution, depletion of natural resources,  
38 soils deterioration are all capable of increasing humanmortality that mean re-  
39 ducing life expectancy (Elo and Preston, 1992; Pope, 2000; Pope et al.,2004  
40 and Evans and Smith, 2005)

41 In deaths and LE, the sex differences vary from country to country or any  
42 region to region. But, in most countries, generally male live shorter lives than  
43 that of female, sometimes by a margin of as much as 5-10 years. This study  
44 was investigated that the LE for female would be higher compared to male in  
45 Bangladesh. The deaths for women were found lower than that of men for all  
46 ages. In general, more boys than girls die in infancy period and during each

1 subsequent years of life,; mortality for male exceed than that of female (Islam,  
2 2003). As a consequence, the gender difference would be more broadened in  
3 the future of the country.

## 6 **Conclusions**

8 In this paper, it is observed that LE for the population of urban area in  
9 Bangladesh follow a simple linear regression model. It is investigated that the  
10 significance of these constructed models is very soaring because of test  
11 statistics-F. Then, LE for the population of male, female and both sexes of  
12 urban area in Bangladesh are projected using these models during 2012-2051.  
13 It is also observed that people in Bangladesh tend to have substantial longer  
14 life expectancy rate. These might be used as predicted LE for the population of  
15 male, female and both sexes of urban area in Bangladesh for 2012-2051 for  
16 further higher study. The LE for the population of male, female and both sexes  
17 of urban area in Bangladesh in 2051 will be 75, 84.1 and 78 years respectively  
18 which exhibits that the urban population of Bangladesh are radically tending to  
19 be old aged population. Proper planning for the allocation of public and private  
20 resources may be taken based on the findings of this study for the better  
21 lifestyle of urban residents. More research study should be needed in this arena.

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