

Astronomy of the Earth-Moon system and the Eschatological Expectations of the Christian Historians of the 5th Century CE

This is a historian's view of how modern astronomy data can be used to discuss the shifting historical worldview of Late Antiquity. In this article an attempt is made to construct an approximate model of how the cycles of astronomical bodies' visible rotation affected the writing of history and self-representation of the Roman empire's powerful people. It is argued that while rare outstanding events like solar eclipses might have caused a short stir in the minds of the rulers and their environment, long-term cycles based on the synchronization of the Moon's phases with the solar calendar and the cycles of the planets lining up in the same disposition (in relationship to the Moon or without this relationship) were the foundation of astronomy-based Christian chronological system. The emergence of the Christian historical worldview in the 5th century was marked by appearance of a significant eschatological strain in it. Historians paid attention not only to the theology-defined signs of the end of the world, but also, as it has been suggested in modern studies, to the some outstanding celestial phenomena. In this paper I would like to address several criteria which may help understand what in the celestial motions interested the astronomers and historians of the 5th century. This paper uses the first approximation of astronomical data for solving the problem of how relevant the skies were for historians, although all numeric parameters are taken from the up-to-date astronomy reference publications. It is an attempt to understand whether the very basic approximations can be related to what historians know from the array of sources available to them. The analysis suggests that there is a whole array of occasions when the dates of astronomical events, received with the help of these basic approximations, coincide with the data from historical sources.

In Late Antiquity, Christian history emerged from the traditional to the Classical Greek and Roman world historiography. Historians started to reconcile biblical chronology with their own since the the time of Hellenism.¹ Julius Sextus Africanus made a significant effort in the 3rd century to produce an uniform chronology of the Old Testament and of the Christian era.² The writing of Eusebius, Ammianus Marcellinus, Orosius, Sozomenos, Socrates, Philostorgios, Hydatius, Sulpicius Severus, and Prosper of Aquitaine created a

¹Wacholder, Ben Zion. "Biblical Chronology in the Hellenistic World Chronicles". In: *The Harvard Theological Review* 61.3 (1968), p. 451–452.

²Sextus Julius Africanus. *Chronographiae: The Extant Fragments*. Ed. by Wallraff, Martin et al. Berlin-New York, 2007; Gelzer, Heinrich. *Sextus Julius Africanus und die byzantinische Chronographie*. Hildesheim, 1885-1898. 283, 500; Mosshammer, Alden. "The Christian Era of Julius Africanus: With an Excursus on Olympiad Chronology". In: *Julius Africanus und die christliche Weltchronistik*. Ed. by Wallraff, Martin. Berlin, 2006, p. 83–112; Mosshammer, Alden A. *The Easter computus and the origins of the Christian era*. Oxford early Christian studies. Oxford, 2008. 474 pp.

1 foundation in the form of a chronicle.³ Theologians like Augustine and the
 2 historians who followed in his path (Orosius, Hydatius, Sulpicius Severus,
 3 Prosper of Aquitaine) contributed to write a new historical narrative that
 4 superimposed the Christian vision of history, with its resonant eschatological
 5 theme, on the histories of the Roman empire and the regions comprising it. The
 6 presence of eschatology in historical thinking was addressed by Richard
 7 Landes, who argued that it was indeed an important cultural and religious
 8 paradigm for the Christians since the 5th century.⁴

9 In a recent study it was suggested that the astronomical phenomena took a
 10 significant part in the narrative structure of the 5th-century historians. Thus
 11 Hydatius' observing the blood Moon of 462 CE (a usual phenomenon when the
 12 Moon is its perigee) was placed in the context of the barbarian ruler, Euric,
 13 grabbing the power in Spain in 467 CE and the failed naval expeditions of Leo
 14 and Anthemius in 468 CE.⁵ Thus this Iberian historian successfully put the
 15 eschatology as an abstract context to the test of the astronomical observation. It
 16 has also long been noticed that in the 8th century Venerable Bede paid
 17 attention to the fact that during one of the eclipses of the 7th century the Moon
 18 reached its phase in discord with the Easter tables.⁶

19 In the light of the new advances in the astronomy I would attempt to draw
 20 attention to one particular coincidence that may theoretically serve as an
 21 explanation of the 5th-century' particular disquietude in the writing of history.
 22 Many studies have laid the theoretical groundwork for solving the problem of
 23 the Earth-Moon system in precise mathematical terms.⁷ An analysis of these

³Brooks, Deanna. "Prosper's Chronicle: A Critical Edition and Translation of the Edition of 445". PhD thesis. Ottawa: University of Ottawa, 2014; Burgess, Richard. *Studies in Eusebian and Post-Eusebian Chronology*. Historia Einzelschriften 135. Stuttgart, 1999; Burgess, R. "Chronicles, Consuls, and Coins: Historiography and History in the Later Roman Empire". In: London, 2011; Burgess, Richard. "The Chronograph of 354: Its Manuscripts, Contents, and History". In: *Journal of Late Antiquity* 5.2 (Jan. 2012), p. 345–396; Burgess, Richard W. and Dijkstra, Jitse H. F. "The Berlin 'Chronicle' (P.Berol. inv. 13296): A New Edition of the Earliest Extant Late Antique Consularia". In: *Archiv für Papyrusforschung* 58 (2012), p. 273–301; Burgess, Richard and Kulikowski, Michael. *Mosaics of Time: The Latin Chronicle Traditions from the First Century BC to the Sixth Century AD*. Turnhout, 2013; Croke, B. "The origins of the Christian world chronicle". In: *History and historians in Late Antiquity*. Ed. by Croke, Brian and Emmett, Alanna M. Sydney, New York, 1983, p. 116–131; Croke, Brian. "Cassiodorus and the Getica of Jordanes". In: *Classical Philology* 82.2 (1987), p. 117–134; Croke, Brian. "Jordanes and the Immediate Past". In: *Historia: Zeitschrift für Alte Geschichte* 54.4 (2005), p. 473–494; Zecchini, G. "Latin Historiography: Jerome, Orosius and the Western Chronicles". In: *Greek and Roman Historiography in Late Antiquity: Fourth to Sixth Century A.D.* Ed. by Marasco, G. Leiden, 2003, p. 317–345.

⁴Landes, Richard. "«Millenarismus absconditus»: L'historiographie augustiniennne et le mill'endarisme du haut Moyen Age jusqu'a l'an Mil". In: *Le Moyen Age* 98.3-4 (1992), p. 355–377; Landes, R. "Sur la traces du Millenium: la «via negativa»". In: *Le Moyen Age* 99.1 (1993), p. 5–26; Landes, Richard. "In the Fear of an Apocalyptic Year 1000: Augustinian Historiography, Medieval and Modern". In: *Speculum* 75 (2000), p. 97–145.

⁵Wieser, Veronika. "The Chronicle of Hydatius: A Historical Guidebook to the Last Days of the Western Roman Empire". In: *Apocalypse and Reform from Late Antiquity to the Middle Ages*. Ed. by Gabriele, Matthew and Palmer, James T. Abingdon, Oxon, 2018, p. 21.

⁶Moreton, Jennifer. "Doubts about the Calendar: Bede and the Eclipse of 664". In: *Isis* 89.1 (1998), p. 50–65.

⁷Euler, Leonard. "De motu nodorum lunae eiusque inclinationis ad eclipticam variatione [E138]".

1 theories was summarized by F. Tisserand.⁸ By 1984 modern measurements and
 2 calculation methods removed all empirical terms from the Moon's ephemeris.⁹
 3 The information gained with the help of modern methods has now been put up
 4 for academic use at various sites including the NASA eclipse site ([https://ecli](https://eclipse.gsfc.nasa.gov/)
 5 [pse.gsfc.nasa.gov/](https://eclipse.gsfc.nasa.gov/)). This allows a historian to investigate whether history and
 6 the astronomical calculations can be both employed to make judgment about
 7 the chronology of Late Antiquity. The approach employed in this paper is a
 8 first approximation, based on the modern data.

9 The question that arises when a historian looks at the astronomical
 10 information for the period is a dichotomy of what was more important for the
 11 astronomers in Late Antiquity, the rare and singular, but spectacular events like
 12 solar eclipses or the periodic events like regular lunar phases at expected
 13 periods of time and planetary line-ups. It is a long-standing question whether
 14 scholars in Antiquity managed to find a way to include solar and lunar eclipses
 15 into a pattern of a calendar. In other words, it is a question of whether people of
 16 Late Antiquity chose to be scared of the rare celestial events and to interpret
 17 them as divine punishment or they favored stability and made a system of
 18 continuing and repeating events. I argue that the patterns of lunar, planetary,
 19 and stars' motion played a much larger role than the eclipses. In other words,
 20 the periodic motions that were possible to predict with reasonable accuracy
 21 played a much more significant role in the relationship of people to the
 22 astronomical events than did the eclipses. The basis of calendars were the
 23 repeating motions of the celestial objects.

24 Let us first consider the arguments about the importance of eclipses for
 25 astronomers' and rulers' views on history.

26 Eclipses, the events that stood out of the calendric patterns in Late
 27 Antiquity, did not seem to be associated with the Modern scholars have long

In: *Novi Commentarii Academiae Scientiarum Imperialis Petropolitanae* 1 (1750), 387–427 + Tab. 16, Fig. 1–2; Euler, Leonard. *Theoria motus lunae exhibens omnes ejus inaequalitates In additamento hoc idem argumentum aliter tractatur simulque ostenditur quemadmodum motus lunae cum omnibus inaequalitatibus innumeris aliis modis repraesentari atque ad calculum revocari possit auctore L. Eulero Impensis academiae imperialis scientiarum Petropolitanae anno 1753 [E187].* St.Petersbourg, 1753. 347 pp. (henceforth cited as Euler L. *Theoria motus lunae*. 1753.); Hansen, Peter Andreas. *Fundamenta nova investigationis orbitae verae quam Luna perlustrat.* Gotha, 1838; Newcomb, S. *Astronomical papers prepared for the use of the American ephemeris and nautical almanac.* Vol. 6: *Tables of the Four Inner Planets.* Washington, DC, 1898; Brown, E. W. *An Introductory Treatise on the Lunar Theory.* Cambridge, 1896; Brown, Ernest W. "The Evidence for Changes in the Rate of Rotation of the Earth and Their Geophysical Consequences". In: *Proceedings of the National Academy of Sciences of the United States of America* 12.6 (1926), p. 406–413.

⁸Tisserand, Félix. *Traité de mécanique céleste.* Vol. 3. Paris, 1894.

⁹Meeus, J. and Savoie, D. "The History of the Tropical Year". In: *The Journal of the British Astronomical Association* 102.1 (), p.40–42; Meeus, Jean. *Astronomical Algorithms.* 2nd ed. Richmond, VA, 2009; Morrison, L. V. and Stephenson, F. R. "Historical Values of the Earth's Clock Error ΔT and the Calculation of Eclipses". In: *Journal for the History of Astronomy* 35.3 (2004), p. 327–336; Simon, J. L. "Numerical expressions for precession formulae and mean elements for the Moon and the planets". In: *Astronomy and Astrophysics* 282 (1994), p. 663–683; Seidelmann, P. K. *Explanatory Supplement to the Astronomical Almanac.* Mill Valley, 1992, p. 317.

1 known two major solar eclipses in the reign of Nero on April 30, 59 CE and in
 2 the reign of Constance II in 346 CE (we have shown why the latter was
 3 important earlier). One may wonder whether such natural phenomena could
 4 have influenced the underlying stability of human perception of time. In
 5 regards to the eclipse of Nero's time, Tacitus mentioned that even the Sun
 6 chose to hide from the human sight in light of the emperor's killing of his
 7 mother (Tac. 14:12; Pliny Hist. Nat. 2:70).¹⁰ But there was nothing of this kind
 8 in 346 CE when the eclipse was total for at least one area of the Roman empire,
 9 Antioch.¹¹

10 The examples of astronomical information one can find in the works of
 11 Late Antique chroniclers and their continuators suggest that the facts of
 12 eclipses became part of the historical narrative tradition and even started to
 13 have some eschatological meaning by the end of the 4th century and that
 14 historians learned how to describe their influence on the populace and troops
 15 correctly. But although they took heed to celestial phenomena, they left the
 16 attempts to find a mathematical rule to later generations. Jerome included an
 17 eclipse in his chronicle without a correct date, so the possible candidates are
 18 June 6, 346 CE or October 9, 348 CE. In the 19th century scholars thought the
 19 eclipse of 346 CE to have been visible throughout the Roman empire, while
 20 recent studies suggest its totality spot was in Antioch.¹² But according to
 21 modern calculations there must have been several eclipses in the vicinity of this
 22 date, which must have been visible to at least some residents of the Roman
 23 empire: these were the eclipses of the years 341, 344, 345, 346, 348, 349, 351,
 24 354, 355, 356, 358, 360.¹³ The 346 CE eclipse reached the phase of totality
 25 only in Antioch, as scholars think now, and other eclipses may have been even
 26 less visible in Constantinople. The eclipse of 346 is cited in the early 9th-
 27 century chronicle of Theophanes the Confessor, but it is a much later text that
 28 must have had its antecedents in regards to this information. Some scholars
 29 believe that the original text that mentioned the eclipse was written by
 30 Eusebius of Caesaria's pupil Eusebius of Emesa (ca. 330–ca. 360 CE).¹⁴ This
 31 4th-century scholar was a court astrologer for emperor Constance II, in
 32 addition to being considered one of the important theologians of his period.
 33 Since he was accused of sorcery, it may well be that it was during his tenure as
 34 the court astrologer that several partial and annular solar eclipses took place

¹⁰Lynn, W. T. "Solar Eclipses in the Reign of Nero and Constantine". In: *The Observatory* 16 (1893), p. 294–295; Tacitus. *Annals*. Leipzig, 1978, 14:12; Pliny the Elder. *Historia Naturalis*. Ed. by Bostock, John and Riley, H. T. London, 1855, 2.70.

¹¹Hayakawa, Hisashi, Murata, Koji, and Sôma, Mitsuru. "The Variable Earth's Rotation in the 4th-7th Centuries: New ΔT Constraints from Byzantine Eclipse Records". In: *Publications of the Astronomical Society of the Pacific* 134.094401 (Sept. 2022), p. 3–5.

¹²Lynn, "Solar Eclipses in the Reign of Nero and Constantine"; Hayakawa et al., "The Variable Earth's Rotation", p. 3–5.

¹³Espenak, Fred and Meeus, Jean. "Five Millenium Catalog of Solar Eclipses: -1999 to +3000 (2000 BCE to 3000 CE) (NASA Technical Publication NASA/TP-2006-214141)".

¹⁴Reidy, J. J. "Eusebius of Emesa and the "Continuatio Antiochiensis Eusebii"". In: *Journal of Ecclesiastical History* 66 (2015), p. 471–8; Burgess, *Studies in Eusebian and Post-Eusebian Chronology*, p. 273.

1 (Wynn, 2011). In other words, the information about the 346 CE eclipse (or
 2 several eclipses), which might have had eschatological underpinning did not
 3 enter the historians' parlance and became the matter of historical narrative only
 4 well after the reign of Constantius II had ended and after the Roman empire in
 5 the West had ceased to exist.

6 In contrast, Ammianus Marcellinus more precisely pinned down the
 7 eclipse in the year 359 or 360 CE in his "Res gestae" 20.3.1-2 and, unlike
 8 Jerome, spoke of the nearly eschatological outcome of this event for the
 9 Roman army.¹⁵ Some scholars believe his description to be impeccable from
 10 the point of view of Late Antique astronomy, while others argue that
 11 Ammianus was not quite correct in discussing the difference between the New
 12 Moon and the eclipse.¹⁶ If we are to believe the dating and his information, it
 13 must have been the eclipse of August 28th, 360. But since Ammianus spoke of
 14 how Julian rallied a large number of Gallic legions to move to take part in the
 15 campaign in the East, the August date seems a bit late. Is it possible that this
 16 historian confused this eclipse with the hybrid eclipse on March 15th, 359, a
 17 year before that? This eclipse (a hybrid one) may better conform to the
 18 description of the historian who spoke of how the Sun's surface was "cut off by
 19 a spear" (*lancea*). In this case the events that had been brought into motion
 20 could have lasted from March 15, 359 to 360, and it was enough time for Julian
 21 to understand tensions among soldiers and procurement problems and to make
 22 a decision to propose them to go on a campaign in the East with their wives.
 23 The requirement to arrange for public postal carts for them to relocate also
 24 required a significant amount of time. In other words, it seems that in
 25 Ammianus Marcellinus' narrative the eclipse took a significant place as an
 26 event that caused some stir in Gaul. Thus unlike Jerome, who shunned from
 27 giving any social commentary on what the eclipse might have caused in the
 28 population, by the end of the 4th century a historian could venture on
 29 describing what a celestial event meant for the Roman army in the West, where
 30 the eclipse was the most pronounced. Ammianus, in contrast to Jerome, already
 31 became well-versed in the writings of Ancient and contemporary astronomers
 32 as to explain the reasons for an eclipse in a clear Latin.¹⁷ He may have made
 33 even more use of it because the eclipse served as a kind of forewarning of
 34 Julian becoming a usurper. It seems that the authorities' and community's
 35 response to such events only became sensible if there was a consensus among
 36 the the powerful people and scholars on how to react to celestial events.
 37 Ammianus' approach to this event suggests that this consensus was becoming
 38 crystallized, as an out-of-order celestial event became a commentary on the
 39 out-sized ambition of formerly modest Caesar.¹⁸ Other remarkable eclipses of
 40 418 CE (described by Philostorgius) and of 484 CE show that historians

¹⁵Ammianus Marcellinus. *Rerum gestarum libri qui supersunt*. Ed. by Seyfarth, Wolfgang. 2 vols. Leipzig, 1978 (henceforth cited as *Amm. Marc. Rer. gest.*).

¹⁶Szidat, J. *Historischer Kommentar zu Ammianus Marcellinus Buch XX-XXI. Teil I. Die Erhebung Julians*. *Historia Einzelschriften* 31. Wiesbaden, 1977, p. 20.3; Hengst, D. den. "Ammianus Marcellinus on Astronomy (Res Gestae 20.3)". In: *Mnemosyne Fourth Series* 39 (1/2 1986), p. 141.

¹⁷Szidat, *Historischer Kommentar*, p. 20.3.

¹⁸Szidat, *Historischer Kommentar*, p. 21.5.1.

1 learned how to make sense out of celestial events, but also managed to stay
2 clear of the overarching conclusions with eschatological implications.¹⁹ In
3 other words, by the early 5th century eclipses and the conjunctions of the lunar
4 calendar with the solar one became a phenomenon historians could include in
5 their narratives and even make it a sign of the Christian history approaching a
6 predetermined stage.

7 One may construct an argument that astronomers sought how to
8 accommodate the eclipses into the repeating patterns of time. But the task of
9 predicting them was largely impossible. Instead, by the end of the 4th century
10 historians managed to construct a language that would help them describe solar
11 eclipses as both natural and social phenomenon, the latter having strong
12 eschatological notes. The eschatological aspect of these commentaries betrayed
13 in the first place a desire either to fit an event into an already functioning set of
14 cycles as a real marker of a repeating phenomenon or to discard it as a
15 meaningless fluke.

16 In other words, the introduction of Christianity as the official religion and
17 of its lunisolar calendar may have been responsible for making scholars pay
18 more attention to the correlation of the Sun and the Moon's cycles and their
19 calendars. This did not happen because they forewarned the "judgment of
20 Heavens", but for another reason, I believe. What was more important were the
21 repeating patterns in the motions of the Sun and the Moon together, or rather,
22 the situations when the lunar phases fell on the same days of the lunar calendar
23 as it did at some historically or symbolically important date like the foundation
24 of the Temple by David or the birth of Christ. The specialists in time reckoning
25 knew about the repeating patterns of 19 and 76 years. Solar and lunar eclipses
26 fell out of this pattern and they were hard to predict due to their irregularity at a
27 given location. In other words, I argue that the solar eclipses that were hard to
28 predict were not interpreted as part of a picture of universal history, on which a
29 community's self-representation was built. But the repeating patterns of the
30 conjunctions of the solar and lunar calendars did indeed attract more
31 attention than solar eclipses from astronomers and historians, who seemed to
32 attempt to align the political events with the conjunctions of the solar and lunar
33 calendar.

34 Because the astronomers of Late Antiquity may not have known that the
35 actual length of the year was 365.24219 days and that the lunar month was
36 actually 29.53 solar days (29½ days plus ca. 43 minutes), there accumulated in
37 calendars a small but significant discrepancy. If the discrepancy was not
38 counted in, the solar calendar lost one day over the course of about 276 years.
39 This seemed to be the problem of the Egyptian and of the Julian calendars,
40 which held the length of the year to be exactly 365 and a quarter day. The same
41 happened to the calendar of the Moon phases and the projected calculations
42 must have been routinely off the actual phase of the Moon at the expected time
43 on the given day of the solar calendar.²⁰ Since the precession data is

¹⁹Hayakawa et al., "The Variable Earth's Rotation in the 4th-7th Centuries", p. 5–7.

²⁰Locher, Kurt. "Long-term Variation in the Motions of the Earth and the Moon". In: *Ancient Egyptian Chronology*. Ed. by Hornung, Erik, Krauss, Rolf, and Warburton, David A. Leiden, 2006,

1 incorporated into most modern calculations,²¹ we will not be using it directly.
 2 For the purposes of advancing our hypothesis we will using the modern mean
 3 values. In the long run, as we will show, the mean values provide a fairly good
 4 approximation to explain how the celestial bodies were visible to astronomers
 5 and people in Late Antiquity. Let us use a simplest model here without
 6 employing the ΔT calculations. These will be at first purely hypothetical
 7 considerations which we will later compare with the data available to us from
 8 historical sources. This approach is justified because it is from the historical
 9 sources that modern astronomers take the first information to construct their
 10 models.

11 The mathematical formula for that is ('i' is the integer number of years):
 12 $((i \times 365.24219) \bmod 29.53) \leq 0.25$ or $((i \times 365.24219) \bmod 29.53) \geq 29.27$,
 13 which means a conjunction of the synodic positions of the Sun and the Moon
 14 within $\frac{1}{4}$ of a day, that is, within 6 hours. The case in point here are the
 15 calculations that would be made from the year 1 BCE as the measure of the
 16 Moon's phases across the Julian calendar's year roll. If we take the actual
 17 astronomical solar year and the lunar month, then, without the imprecision that
 18 the human-made calendar introduced, there were several dates when the solar
 19 and the lunar rotations coincided. These were the years 19 (the foundation of
 20 the Easter calendar), 38 (two 19-year cycles), 57, 76, 483, 502, 521, 540, 559,
 21 578 and 598. Let us notice that there was a long hiatus of 3 centuries when the
 22 phase of the Moon did not repeat its showing on 1 BCE in regards to the same
 23 dates of the Solar, Julian (or in some cases, proleptic Julian) calendar. Let us
 24 also notice that several dates fall in the late 5th and the early 6th century, the
 25 period that was marked by the Fall of the Roman Empire in the West, the re-
 26 fashioning and consolidation of the Byzantine empire in the East and by the
 27 creation in the West of several barbarian kingdoms. Frankish king Clovis I
 28 came to power in 481 CE and was gradually gaining his prestige, ultimately
 29 defeating Syagrius in 486. The year 483 was also important because it was
 30 close to the cycle of precession of 476 years that L. Euler mathematically
 31 calculated. It was also the year when the Easter calendar had to be adjusted to
 32 take one day off the count of lunar epacts.²² The year 521 CE was the time
 33 when early medieval scholars started thinking about the new Easter calendar
 34 that was later confirmed and realized by Dionysius Exiguus. 540 CE witnessed
 35 the peak of Byzantine military campaigns of Belisarius, ordered by Justinian.

36 In addition to that, there was a discrepancy between the astronomical
 37 calendar and the Julian calendar, which could become expressed in days. But in
 38 some cases the problem was less in the actual count of days since in the
 39 Ancient world the astronomers managed to create calendars that helped

p. 398.

²¹Simon, J. L. et al. "Numerical expressions for precession formulae and mean elements for the Moon and the planets". In: *Astronomy and Astrophysics* 282 (1994), p. 663–683.

²²Euler, Leonard. *Theoria motuum lunae, novo metodo pertractata una cum tabulis astronomicis, unde ad quodvis tempus loca lunae expedite computari possunt incredibile studio atque indefesso labore trium academicorum: Johannis Alberti Euler, Wolffgangi Ludovici Krafft, Johannis Andreae Lexell. Opus dirigente Leonardo Eulero acad. scient. Borussicae direttore vicennali et socio acad. Petrop. Parisin. et Lond. [E418].* Petropoli, 1772. 775 pp., 400, §379.

1 intercalate any extra days into the year (with an embolismic month and a *saltus*
 2 *lunae*). The problem also lay in the extra hours that cumulatively added up
 3 from the minutes and seconds of the discrepancies between the Julian solar
 4 calendar and the Ancient world's lunar calendar with the actual astronomical
 5 phenomena. These discrepancies between the astronomical calendar and the
 6 Julian calendar can be calculated at the first iteration with the help of the
 7 modern data for the parameters of the Earth's and Moon's orbits. The simplest
 8 mathematical formula that is used here is of the following form: $|((i \times$
 9 $365.24219) \bmod 29.53) - ((i \times 365.25) \bmod 29.5)| \leq 0.25$. Its use is justified as
 10 the first iteration approach to the problem and is supported by works on
 11 astronomy from Leonard Euler on. The actual astronomical conjunction of the
 12 Moon's phase with the solar synodic position in this case came on
 13 approximately the following years: 77, 156, 233, 312, 390, 467, 544, 623, 700,
 14 778. Thus one may notice two separate sequences: one of purely astronomical
 15 conjunctions, some cycles of which govern the lunisolar calendar today, and
 16 the other of the correlations (with half a day precision) between the
 17 astronomical and the Julian calendar. These sequences do not count in the
 18 longer precessions of the Earth's and Moon's rotation with the length of 1000
 19 years and so on, but L. Euler's works on the Earth-Moon motion showed that
 20 these periods do exist in the heuristic observations and calculations with all
 21 types of precession included as a parameter. These years are themselves an
 22 approximation as normally there were several years in the vicinity of each of
 23 these cardinal dates when the Moon's phases were within one day of those in
 24 the year 1 BCE as measured against the Julian calendar. It can be argued that
 25 the most common average period when both the astronomical conjunction and
 26 the correlations between the astronomical and Julian calendars took place was
 27 between 72 and 84 years, with the most weight of the phenomenon falling on
 28 76 years.

29 The question of employing the conjunction of the solar and lunar calendars
 30 for the better observation of the Moon's phase seemed to have bothered
 31 historians and computists since the 4th century. Of the dates of the conjunction,
 32 two (313 CE and 390 CE) are quite close to the two most egregious cases in
 33 Jerome and Prosper's chronicles where they either hinted at or showed a one-
 34 year discrepancy with other sources. Eusebius put the battle of the Milvian
 35 bridge at the 7th year of Constantine, which was 312 CE, while Jerome set it to
 36 the 6th year of Constantine, although it was also 312 CE, since he had set the
 37 1st year of Constantine at 307 CE.²³ In this case the Moon's calendar for 312
 38 CE and for 313 CE was within one-day's precision in regards to the
 39 calculations from the year 1 BCE, but the difference was, respectively, 4 and
 40 13 hours. So Jerome's indecision to choose between the 2 dates is
 41 understandable as he sought to move the start date of the count so as to make
 42 the discrepancy less. Exactly 6 years had a discrepancy of only 6 hours with
 43 the year 1 of Constantine, while the year 7 had a much larger discrepancy of 15
 44 hours. So for an important event like the battle of the Milvian bridge he needed
 45 that it be at the beginning of the year 6 of Constantine so that the position of

²³Burgess, *Studies in Eusebian and Post-Eusebian Chronology*, p. 43.

1 the Moon be predictable in the the terms of the conjunction between the solar
 2 and the lunar calendars. L. Euler in the 18th century determined one cycle of
 3 the Moon's motion to be 6.5 years, which explains that there was a conjunction
 4 of the Moon's position in the middle of the 7th year, but before its end.

5 Prosper of Aquitaine, in turn, moved the events from 383 CE to 384 CE.²⁴
 6 The shifting of an event from 383 CE to 384 CE was meant better to account
 7 for the fact that in terms of the lunar phases, the Solar calendar was running out
 8 of sync in 383 CE and it came in sync by 384 CE. In his case the reason might
 9 have been that in the year 383 CE the discrepancy was 9 hours, while in the
 10 year 384 CE the Moon reached near total conjunction with its position in the 1
 11 BCE in terms of hours, while the visible lunar epact had grown by 2 days. In
 12 other words, the Full Moon could be seen at the same time at night as it was in
 13 1 BCE. This was the case for the years 389 CE and 390 CE, too, where the
 14 discrepancy between the calculated position of the Moon and its real phase was
 15 minimal (plus 3 and minus 5 hours respectively). It is quite likely that full days
 16 did not bother computists (the specialists in the calculation of the date of
 17 Easter) at all since there were mathematical means to account for them. Thus
 18 one may notice that since the 4th century, when Christianity and its lunisolar
 19 calendar became official, historians did care about using the dates for which
 20 the projected correlation between the motions of the Moon and the Sun was in
 21 nearly total sync with their visible correlation. In other words, the first two
 22 centuries of the Christian Roman empire raised a number of significant
 23 challenges for historians and computists because they had to address the
 24 problem of making a time to observe the Moon at the time when its phase
 25 coincided with the expectations made of the basis of the "Egyptian" calendar.
 26 In discussing the problems of the Christian time reckoning in the 4th and 5th
 27 century one may consider the discrepancy that emerged because of the actual
 28 astronomical calendar having a shorter year than the one used in the Egyptian
 29 and Julian calendars.

30 In other words, I argue that the innate 76-year cycle in the Earth-Moon
 31 system's motion and the patterns of the Moon's phases exactly coinciding with
 32 the dates in the Solar calendar (like the Vernal equinox) and thus taking the
 33 same relative position in the sky against the immovable objects on the ground
 34 (temples) made astronomers and historians look after the solar eclipses with
 35 increased attention. It was not vice versa.

36 One may also consider another factor in discussing how the celestial
 37 events might have influenced the vision of history among the educated people.
 38 In addition to the conjunctions of the solar and the lunar motions one may also
 39 consider the lineup of planets in the same form as a possible marker of
 40 information the astronomers gathered by looking at the skies. Although the
 41 lineups of planets are a common event, the cases in which it took place on the
 42 same date of the solar calendar are much more rare. The conjunction with the
 43 solar calendar is important because it is connected to the Vernal equinox,
 44 which had been observed for the purpose of relating the solar and the lunar

²⁴Humphries, Mark. "Chronicle and Chronology: Prosper of Aquitaine, his methods and the development of early medieval chronography". In: *Early Medieval Europe* 5 (1996), p. 166.

1 calendar to each other. For the purposes of this paper I will only consider cases
 2 when the lineup of planets was observed during a solar eclipse, since there is
 3 very little information on what astronomers saw in the night skies on usual
 4 days. Thus we need to consider the eclipses of the Ancient world as the
 5 possible starting points of observation when the astronomers remembered the
 6 configuration and made it a historical point of reference. These cases are
 7 visible with the help of modern astronomical tables that use the advanced
 8 mathematics developed since the 17th century.

9 There is another reason for the years in the vicinity of 476 CE (like 468
 10 CE and 483 CE) being of interest to astronomers and historians of Late
 11 Antiquity. In terms of the astronomical observations the 5th century was
 12 special because during it the long-term cycles of the Earth's and other planets'
 13 motions had come to a synchronization. The rotation of the planets around the
 14 Sun makes them line up in various configurations in the skies visible from
 15 Earth. Already in the 13th century BCE the Egyptians were watching the
 16 planets.²⁵ The period in which a planet returns to the same point in the skies as
 17 visible from Earth (the synodic period) has now been precisely calculated by
 18 astronomers. The synodic periods for Earth, Jupiter and Saturn are very close,
 19 while the periods for Venus and Mars differ significantly. As the first
 20 approximation of solving this problem is the approach which seeks to establish
 21 the level of synchronicity of the planets' synodic periods by examining their
 22 periodic qualities against that of the Earth's orbit and of the solar year. But we
 23 are interested not in all the lineups, which happen regularly about every 20
 24 years, but only in those that happen at exactly the same date as the original one
 25 (say, the New Year, the Vernal Equinox, 1st September, or any other civic
 26 holiday). If one calculates the offsets, i. e. the discrepancies between the length
 27 of the solar year and synodic period for each planet, this data can be used to
 28 determine when the planets would reappear in the same order and at the same
 29 visual distance from each other as they had once been observed. Naturally,
 30 those years when the offset is the smallest are the years when the configuration
 31 of the planets was the same. Setting the offset to within 3 to 4 months is a
 32 reasonable assumption. There is a further option to take the offsets, calculate
 33 the geometric mean and to calculate the mean square deviation for each of the
 34 planets' offsets. Finding the years when this mean square deviation is less than
 35 a month is a good technique to find those years when the planets were in the
 36 same line-up as initially. Interestingly, both methods give approximately the
 37 same results. For the purposes of this paper the possible precession of the
 38 planets' synodic position due the Earth's precession against the fixed stars is
 39 not considered since it is the first approximation and since the proposed
 40 method does give heuristically verifiable results within the given limits of
 41 approximation.

42 Calculations would not mean much if we would not set a starting point.

²⁵Krauss, R. "The Eye of Horus and the Planet Venus: Astronomical and Mythological References".
 In: (). Ed. by Steele, J. M. and Imhausen, A., p. 144; Krauss, Rolf. "Dates Relating to Seasonal
 Phenomena and Miscellaneous Astronomical Dates". In: *Ancient Egyptian Chronology*. Ed. by
 Hornung, Erik, Krauss, Rolf, and Warburton, David A. Leiden, 2006, p. 378.

1 Solar eclipses in Antiquity are a good starting point since during an eclipse the
 2 line-up of planets became visible during the day and attracted attention of the
 3 educated people and the populace. Once remembered, this line-up could have
 4 long stayed in memory. The ancient documented solar eclipse of 2161 BCE
 5 (Huber, 1999), that of Shamshi-Adad of 1587 BCE (probably the eclipse of
 6 Oct. 23, 1588 BCE or of Mar. 28th, 1586 BCE),²⁶ the recorded eclipse of Sep.
 7 11, 1557 BCE,²⁷ the lunar eclipse of 1547 BCE (the Ur III eclipse),²⁸ the
 8 lesser-known solar eclipse of Feb. 15, 1547 BCE,²⁹ the solar eclipses of Oct.
 9 30th, 1207 BCE (Joshua 10:12-13),³⁰ 1096 BCE and 1084 BCE (March 27th)
 10 may be taken as possible candidates. To understand which of the starting points
 11 is better one needs to use modern data. For example, since 2023 is the year of
 12 the planets' line-up, it is remarkable that this configuration of planets repeats
 13 the order that might have been visible during the eclipse of the year 2161 BCE
 14 or of 1084 BCE, but not during the other ones. For the purposes of this paper
 15 we obviously do not count in any planetary precession since these
 16 considerations are the first approximation.

17 Calculations which involve finding those years that have the smallest
 18 offsets in terms of the planets' synodic periods first show the importance of
 19 years in the vicinity of 483 CE. For example, if calculated from the solar
 20 eclipse of 1547 BCE, in 484 CE Jupiter came earlier by 18 days, Venus and
 21 Mars appeared right where they had been in 1547 BCE, while Saturn was early
 22 by 160 days. Let us notice that the Solar eclipse of 484 CE was well observed
 23 (Hayakawa et al., 2022, 5–7). If counted from 1084 BCE, the planetary
 24 configuration repeated in 483 CE and ca. 601 CE, when another eclipse was
 25 visible in the Mediterranean.³¹ If calculated from the Solar eclipse of 27th
 26 March 1084 BCE, in the year 483 CE Jupiter and Mars both came to the same
 27 position in the sky 116 days ahead, while Venus was ahead by 70 days. In
 28 other words, in the period around Christmas those interested in heavens could
 29 observe the planetary line-up that was around Vernal equinox ca. March 27th,
 30 1084 BCE. This is the result we get if we calculate the offset's absolute value
 31 against the length of the solar year. Using the mean quadratic deviation against
 32 the geometric mean of the offset we get much shorter offsets against that day in
 33 the solar year when these planets seemed the closest to their original position in
 34 the starting year.

35 One of the periods that emerges from calculations of this kind is that of

²⁶de Jong, Teije. "Astronomical Fine-Tuning of the Chronology of the Hammurabi Age". In: *Jaarbericht van het Vooraziatisch-Egyptisch Genootschap „Ex Oriente Lux“* 44 (2013), p. 147–167.

²⁷Henriksson, G. "Astronomical Dating of the Old Babylonian Kingdom". In: (2005). Ed. by Koiva, Mare, Pustynnik, Izold, and Vestnik, Liisa, p. 63–70.

²⁸Banjevic, Boris. "Ancient Eclipses and Dating the Fall of Babylon". In: *Publications of the Astronomical Observatory of Belgrade* 80 (2006), p. 251–257; Banjevic, Boris. "Ancient Eclipses and the Fall of Babylon". In: *Publications de l'Observatoire Astronomique de Beograd* 1 (2006).

²⁹Khalisi, Emil. "The Double Eclipse at the Downfall of Old Babylon". In: (2020), p. 3.

³⁰Vainstub, Daniel, Yizhaq, Hezi, and Avner, Uzi. "The Miracle of the Sun and Moon in Joshua 10 as a Solar Eclipse". In: *Vetus Testamentum* 70 (4-5 2020), p. 722–751.

³¹Hayakawa et al., "The Variable Earth's Rotation", p. 7–8.

1 1107 years. It deserves particular attention because the end of it, if counted
 2 from one of the eclipses of the Ancient world, and also from the founding of
 3 Rome, fell right into the middle of the 4th century. An eclipse could have made
 4 the astronomers notice the same lineup of planets as it was during the past
 5 event. Eclipses like that may have also let the astronomers of Late Antiquity to
 6 pay attention to the celestial events and to notice a flaw in the civic calendar
 7 that made it lose one day over 276 years. A well-known Solar eclipse took
 8 place in Nineveh on June 15th, 763 BCE (it was also the day of the New Moon,
 9 so the two events coincided to produce a sense of darkening in the skies. In the
 10 next year, 762 BCE (761 astronomical year) a Full Moon was on March 22nd,
 11 one day after the Vernal equinox. When a whole sequence of solar eclipses
 12 started in 346 CE, the Full Moon was on March 23rd, one day late. These dates
 13 would have had no specific importance, if the period of 1107 years would not
 14 be remarkable for being one of those periods when the planets showed up in
 15 the same order and position as they were initially. It was the 7th year of the
 16 cycle if the 19-year cycles were counted from 763 BCE and the 6th, if 762
 17 BCE was considered the beginning of the count. The 19-year cycle, if counted
 18 from 762 BCE, started on 340 CE, but there was no near coincidence in that
 19 year. In 341 CE (the 1st year of the new 19-year cycle if 762 BCE was the first
 20 year) the Full Moon came 4 days earlier than in 762 BCE, on March 19. It was
 21 also a year of a solar eclipse.³² In 346 CE, another year of a solar eclipse and
 22 the 6th year of the 19-year cycle counted from 762 BCE, the Full Moon
 23 occurred on March 23rd, one day later than in 762 BCE. It is interesting to
 24 notice that since the Solar calendar was late 4 days in comparison to the
 25 Moon's cycle of rotation in 1103 years (762 BCE to 341 CE) even though this
 26 period was an exact integer number of 19-year periods, it was losing 1 day
 27 every 276 years, a well-known parameter. In other words, in 1102–1109 years,
 28 that is, ca. 341 CE, it became clear that the solar and the lunar calendars in the
 29 way they were counted were asynchronous and that the solar calendar lost one
 30 day to the lunar calendar in 276 years. But naturally, the Egyptian scholars
 31 must have taken some problems out of it during the rule of the Ptolemy's from
 32 305 BCE to 30 BCE and the reform of the calendar under Octavian August
 33 must have adjusted all discrepancies. The problem was in the new discrepancy
 34 that should have accumulated by the 3rd century. In other words, the period of
 35 1107 years made those interested in astronomy take notice of the discrepancy
 36 and of asynchronous character of the calendars. It is all the more important
 37 because this visible disagreement in the calendar (4 days) happened ca. 354
 38 CE, which would be the year 1107 from the founding of Rome in 753 BCE.

39 In both calculations, however, in 483 CE or 484 CE the 4 planets came
 40 close to their line-up in either 1084 BCE or 1547 BCE. If the start date was the
 41 eclipse of 1557 BCE, then in 476 CE the line-up repeated that at the starting
 42 point. Let us notice that one planetary cycle is about 468 years within our

³²Espenak and Meeus, "Five Millennium Catalog of Solar Eclipses: -1999 to +3000 (2000 BCE to 3000 CE) (NASA Technical Publication NASA/TP-2006-214141)"; Hayakawa, Murata, and S^oma, "The Variable Earth's Rotation in the 4th-7th Centuries: New ΔT Constraints from Byzantine Eclipse Records", p. 3–5.

1 simple but rigid criteria (but it is not a repeating one). Thus in the middle of the
 2 5th century the planets lined up as they used to during one of the ancient
 3 eclipses, but also in the same fashion as they were at the birth of Christ.

4 In the repetition of the planets' conjunctions there are also other
 5 heuristically calculable periods of ca. 1054 years, of 1739 years, and of about
 6 3107 years, which give almost complete synchronization within the above-
 7 mentioned set of factors. Depending of the start of the calculation and its
 8 relation to an eclipse (or lack thereof), the years 476 CE, 483 CE or 484 CE
 9 were those of the original line-up that repeated that of 1557, 1084 or 1547
 10 BCE. If the start year was the eclipse of 1207 CE, which the scholars now
 11 attribute to that which is mentioned on the Book of Joshua 10:12-13, it gave 3
 12 historically interesting dates of 337 CE (the death of Constantine the Great),
 13 390 CE and 479 CE, as well as the years in the vicinity of the rule of King
 14 David. In other words, using the Babylonian and Hebrew chronologies,
 15 scholars in the Christian Roman empire might have become aware that in the
 16 5th century there will be one planetary line-up that would exactly repeat that of
 17 the beginning of the actual Hebrew chronology that appeared in contact with
 18 the Egyptian and Assyrian empires. Even though it was a repeating event, it
 19 might have influenced scholars in attracting them more towards observing the
 20 skies. Interestingly, these calculations hint at the intrinsic importance of the
 21 year 1108 BCE (minus 1107 astronomical year), when a lunar eclipse
 22 happened on December 28th. If the calculations of the planetary configurations
 23 were to be applied here, the year 1107 BCE becomes critical because it was
 24 when the planets lined up in the same configuration as they did in 2161 BCE
 25 because it came 1054 years after the latter (and as it has been stated already,
 26 1054 years make the planets return to the same position within days of each
 27 other). Since the eclipse was 3 days away from the start of the new 1107 BCE,
 28 the line-up must have been a nearly perfect match and it might have become a
 29 start of a new year count. Remarkably, it is claimed to be the last year of the
 30 reign of Ramesses X (1111–1107 BCE), which caused a discussion among
 31 scholars. The suggestion advanced by a scholar that his reign lasted longer has
 32 been rejected.³³ When part of the lunar disk was covered by the Earth's
 33 shadow, the astronomers might have noticed one of the planets, probably
 34 Venus, that could have been occulted by the bright edge of the Moon's disk.
 35 That is, with a degree of precision we may hypothesize that the line-up that
 36 people saw in 2161 BCE was also visible for those in late 1108 - early 1107
 37 BCE, and in 405, 457, and 490 CE.

38 These considerations suggest that Late Antique astronomers and historians
 39 built their chronological schemes around long-term repeating patterns in the
 40 showing of the Moon and the planets. Solar eclipses that were harder to predict
 41 fell out of these patterns and did not seem to influence the chronology or
 42 calendar in any way: they were never used as the end of an old era or the
 43 beginning of a new one. But when the solar and the lunar calendars repeated
 44 themselves and the showing of the two celestial bodies happened in sync

³³Krauss, R. and Warburton, D. A. "Chronological Table for the Dynastic Period". In: (2006). Ed. by Hornung, E., Krauss, R., and Warburton, D., p. 493.

1 (although it was the night for the Moon when the Sun was not visible), this
 2 seemed to be the time when scholars and those in power paid more attention to
 3 represent themselves according to the history's plan. Thus one may safely
 4 argue that for the historians of the 5th century astronomy suggested that the
 5 end of times, or at least the end of the long cycles of time, was coming about
 6 since the planets and the Moon lined up at the same time and in the same
 7 patterns that they did at the time of the construction of the temple of David and
 8 of the foundation of Rome. It was a factor that determined the interest to the
 9 eschatological discourse.

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