

## Portfolio Manager Ratings: k-Means and LDA versus Active Outperformance

*Consultants that serve in the benefit of institutional investors assign ratings to investment strategies (portfolios of assets) based on face-to-face interactions and other research activities referred to in the industry as ‘due diligence.’ Economic cycles change, and thus consulting firms often claim that ratings are ‘forward looking,’ reflecting portfolio performance two years into the future. Still managers of retirement accounts, endowments or foundations, make investment decisions for today, six months, or a year forward. In apparent contradiction of fiduciary responsibility, institutional investors would be better off selecting the portfolio strategies rated the lowest, to invest beneficiaries’ funds, as our results show. Ratings only capture predicted outperformance two years forward, when portfolio managers are not shown to consistently exhibit skill. An ‘arbitrage’ of sorts, which investors with information on consultant ratings can take advantage of for up to three years, is to invest funds into portfolio strategies rated the lowest. We use dummy-variable estimation, k-means clustering, and linear discriminant analysis on the betas of fixed income portfolios against eight indices that describe the whole corporate bond credit curve. We discern patterns of outperformance versus the ratings.*

**Keywords:** *relative performance, consultant ratings, k-means clustering, discriminant analysis*

### Introduction

A recently published book by Professor Emeritus Dr. George Bitros of the Athens University of Economics and Business, compares the retirement systems of several countries in the world, to that of Greece. The general conclusion is that a system based on performance, such as that of the United States for example, is more stable in the long run than that of Greece, which merely distributes over time income from younger generations into the older ones. However, a potential flaw of the system in the U.S. is that of pinpointing the responsibility of sound management of retiree funds.<sup>1</sup> Central role in this process is taken by investment advising/consulting firms, which in essence determine the allocation of retiree funds into investment portfolio strategies. This study utilizes established metrics in active management, including beta and information ratio (IR) to assess the efficacy of information produced by Morningstar, in its role as portfolio evaluator and issuer of one-to-five-star ratings. The metrics are crucial for evaluating investment strategies and for understanding how well a portfolio performs relative to its benchmark. **Alpha** measures the excess return of a portfolio compared to its benchmark, offering insight into the manager’s skill in generating returns above the market, as represented by a stated benchmark. **Beta** captures portfolio sensitivity to the market index and quantifies systematic risk.

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<sup>1</sup>Xanthopoulos, A., 2024. The Case of the USA. In: G. Bitros, ed. 2024. Pensions: The Problem and the Solution. Thessaloniki: Epikentro, pp.159–190.

1 **Tracking error** assesses the volatility of a portfolio's active returns, which helps  
2 measure the consistency with which a portfolio manager follows a mandate  
3 relative to the benchmark, while generating active performance. The  
4 **information ratio (IR)**, calculated by dividing alpha by tracking error, reflects  
5 risk-adjusted returns above the market benchmark. It is a key indicator of  
6 whether a manager is adding value relative to risks taken. These metrics are  
7 industry-accepted for evaluating active management strategies as objectively as  
8 possible, in addition to looking at ratings that consulting organizations assign. In  
9 this analysis, alpha in the typical sense is made as small as possible. Several  
10 market indices (eight of them) are used to siphon out as much of the potential  
11 out-of-benchmark performance. We use the betas against eight indices  
12 representing the corporate credit yield curve, as the x-variables and regress them  
13 against IR. Portfolio managers' decisions to buy and sell assets at the various  
14 parts of the yield curve. The assigned ratings should not deviate materially from  
15 the active outperformance generated here as Information Ratio (IR). But they do  
16 as we show, in a manner that does not may point to potential breach of fiduciary  
17 responsibility.

18 Quantitative methods, based on industry metrics above as data, receive  
19 attention in the buy-side of the industry, largely due to the specter of 'Fiduciary  
20 Responsibility' regulation that is put in place by the U.S. Department of Labor.  
21 As a result, proactively assessing the efficacy of ratings has become an integral  
22 part of contemporary portfolio strategy performance measurement. These  
23 methods allow institutional investors to systematically classify strategies based  
24 on performance irrespective of the ratings assigned to strategies. Nevertheless,  
25 few of these studies are made public for understandable reasons. To handle  
26 complexity, financial actors implement machine learning algorithms, clustering  
27 algorithms such as k-Means, and classification techniques like Linear  
28 Discriminant Analysis (LDA)<sup>2</sup>. These techniques are robust approaches for  
29 identifying hidden patterns, improving predictive modeling, and optimizing  
30 investment portfolio selection. The combination of k-Means clustering and LDA  
31 has been extensively researched in several fields such as finance, risk  
32 management, and performance evaluation.<sup>3</sup> The method of k-Means, an  
33 unsupervised learning method, helps distinguish between classes, within the data  
34 according to the similarity of specific attributes, based on some measure of  
35 distance. This method lends itself well to separating investment portfolios by  
36 themselves (unsupervised) according to various characteristics, such as the beta  
37 coefficients and performance measures (risk-adjusted returns). Conversely,  
38 LDA is a supervised approach that is used to classify investment strategies  
39 according to their main characteristics. Here, the 'supervising' attribute is that  
40 of a strategy that has been recommended for investing based on consultant five-  
41 star-rating, and the characteristics are the beta coefficients to eight indices, as  
42 above. We perform both kinds of tests, in addition to running a linear regression

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<sup>2</sup> Hastie, T., Tibshirani, R. and Friedman, J., 2008. *The Elements of Statistical Learning: Data Mining, Inference, and Prediction*.

<sup>3</sup> Alzamil, Z. S., Appelbaum, D., Glasgall, W. and Vasarhelyi, M. A., 2021. *Applications of Data Analytics: Cluster Analysis of Not-for-Profit Data*.

1 of risk-adjusted returns against the eight indices, with ratings as binary (0,1)  
2 variables. We find that (a) the regression dummy variable for the least favorable  
3 Morningstar rating adds the most to the risk-adjusted outperformance  
4 (Information Ratio, IR), (b) discriminant function scores align with actual risk-  
5 adjusted outperformance for strategies not recommended; and these scores work  
6 against outperformance for those recommended, (c) for the five clusters  
7 identified based on outperformance of the current month, six-months forward,  
8 12-months forward and two years forward, combined, we show that risk-  
9 adjusted performance is positively related to the linear discriminant score of  
10 recommendation based on ratings; obscuring the other negative relations  
11 between ratings and outperformance obtained in methods (a) and (b). The results  
12 of this study may be of interest in the regulatory arena of fiduciary responsibility,  
13 a full legal analysis of which is out-of-scope for this study. Briefly, the U.S.  
14 Securities and Exchange Commission and the Department of Labor have  
15 attempted to regulate the payments by various methods imposed on investment  
16 management firms<sup>4</sup>. Morningstar assigns ratings to investment managers, which  
17 are in essence classification schemes that are based on face-to-face interaction with  
18 portfolio managers, and subsequent assignment of ‘Stars’ (one through five, in the  
19 case of Morningstar). This activity may entail fiduciary responsibility, to a degree  
20 that is out of scope. The Investment Adviser’s Act of 1940 prescribes that “advisers”  
21 must evaluate portfolios in a “disinterested” manner that involves “reasonable care  
22 to avoid misleading clients.”<sup>5</sup> The Fiduciary Rule finalized in 2016 under the  
23 Obama administration, broadened the definition of when a person or entity took on  
24 fiduciary responsibilities. Before that time, investment advisors fell outside the  
25 definition of fiduciary, and therefore, kickbacks from rated portfolio managers  
26 toward the rating advisers were not only legal, but common practice. To curb these  
27 practices, DOL’s new ERISA rules expanded the definition of a fiduciary and  
28 created a new method of exempting certain prohibited transactions. The Law was  
29 vacated, in 2018, reinstated in 2024 and immediately challenged in court.<sup>6</sup> The rule  
30 “requires retirement investment advisors to provide prudent, loyal, and honest  
31 advice free from overcharges.”<sup>7</sup>

32 The contributions of this study are that: (i) a set of relatively straight-forward  
33 methods to quantify the efficacy of any ratings of investment managers involves  
34 linear regression with dummy variables, a method that could be easily implemented  
35 as a quality control measure in any firms assigning ratings, (ii) ratings and  
36 outperformance are inversely related in the short run, for possible reasons related to  
37 the business cycle or an assessment-to-rating time gap, in addition to intentional  
38 breach of fiduciary duty, (iii) ratings do mildly align with risk-adjusted  
39 outperformance two years forward, based on an autoregressive level-1 forecast of  
40 Information Ratio; however, investment managers consistently produce negative

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<sup>4</sup>The Office of Compliance Inspections and Examinations, 2005. *Staff Report Concerning Examinations of Select Pension Consultants*.

<sup>5</sup>Barbash B. P., and Massari, J., 2008. *The Investment Advisers Act of 1940: Regulation by Accretion*.

<sup>6</sup>Alsdorf, G., 2024. *DOL Fiduciary Rule Saga Continues: 2024 Fiduciary Rule Halted by Texas District Courts*.

<sup>7</sup>Menickella, B., 2024. *The DOL’s Final Fiduciary Rule is Here. See What’s Inside!*

1 alpha two years hence, (iv) institutional investors may have to wait for two years  
2 before the efficacy of ratings becomes apparent, that is, before better (lesser)  
3 outperforming strategies are rated higher (lower) by consultants, (v) the relation  
4 between consultant ratings and risk-adjusted performance of rated strategies is not  
5 as expected: strategies that based on ratings would have been recommended for  
6 investment should exhibit performance that is higher than those not recommended.  
7 Instead, there are highly recommended strategies that exhibit dismal performance  
8 across time. There appears to be only an imprecise, vague positive relation between  
9 clusters of performance and ratings.

## 12 Literature Review

14 Applying k-means clustering and linear discriminant analysis (LDA)  
15 provides a methodical way to generally assess financial market performance,  
16 improve portfolio allocation, and help the institutional investor select investment  
17 strategies based on performance relative to a benchmark within a comparable  
18 investment peer group.<sup>8</sup> We examine the use of these methods in the finance  
19 literature, particularly in performance metrics, manager selection, and the  
20 assessment of efficacy of consultant ratings. The literature explores empirical  
21 studies that portray the effectiveness of these clustering models, summarizes and  
22 identifies important findings, and points to areas that warrant further exploration.  
23 Understanding the importance of k-Means clustering and LDA in performance  
24 evaluation allows institutional investors to improve their decision-making  
25 process, leading to better-quality portfolio management selection. Several  
26 studies have highlighted the importance of these metrics in determining the  
27 success of investment strategies. Chalmers et al. (2020) examine the impact of  
28 financial intermediaries on investor returns, suggesting that investors who rely  
29 heavily on intermediaries face higher fees and risks without necessarily  
30 achieving superior outperformance. This finding aligns with the broader critique  
31 of traditional investment strategies, where active management often fails to  
32 justify the additional costs. By contrast, focusing on objective metrics like the  
33 information ratio could allow for a more transparent evaluation of portfolio  
34 performance, providing clearer insights into whether managers generate value  
35 beyond the benchmark. The role of classification schemes in influencing  
36 investment decisions has also been widely debated. Many traditional  
37 classification systems rely on outdated or overly simplistic criteria that may not  
38 fully capture a portfolio's potential. This study contrasts such approaches by  
39 introducing machine learning models, trained on data such as rating information,  
40 to predict investment strategy performance. The use of machine learning offers  
41 an opportunity to go beyond traditional classification schemes, uncovering  
42 patterns and correlations in data that might not be evident through conventional  
43 analysis. These models, when applied correctly, could offer more accurate and  
44 dynamic assessments of investment strategies, aligning with the research by

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<sup>8</sup>Roberts, R, Potthast, C. and Dellaert, F., 2009. *Learning general optical flow subspaces for egomotion estimation and detection of motion anomalies.*

1 Gennaioli et al. (2015), who argue that financial advisors often exploit investor  
2 biases, amplifying market volatility. Chalmers et al. (2012) highlight the  
3 conflicts of interest that arise from financial advisors' fee structures, noting how  
4 these incentives often lead to underperforming portfolios. When compensation  
5 is tied to the sale of specific products or services, there is a significant risk of  
6 misalignment with the best interests of the client. In such environments, it is  
7 essential for investors to have access to unbiased recommendations. We support  
8 the argument that machine learning models, by providing more data-driven and  
9 objective evaluations, mitigates some of these conflicts, giving investors better  
10 tools to assess their options.

11 Despite general concerns over potential market destabilization due to these  
12 rating schemes, little publicly available evidence of systemic risks has been  
13 observed in the general literature. Gennaioli et al. (2015) discuss how money  
14 managers often cater to investor biases, which can lead to greater market  
15 volatility and noise trading.<sup>9</sup> However, this research suggests that when rating  
16 schemes are applied transparently, they can contribute to more effective  
17 decision-making by providing a structured framework for evaluating investment  
18 strategies. In our view, rating schemes are not applied very transparently, or the  
19 Department of Labor would have no reason to reinstate the Fiduciary Rule Law. And  
20 the integration of statistical learning models enhances this process by enabling a  
21 more nuanced analysis that considers historical performance, in addition to  
22 consultant ratings. Another significant area explored in the literature is the impact  
23 of institutional investors on investment outcomes. Goyal (2008) demonstrates  
24 that larger institutional investors, who are less reliant on consultants, often  
25 achieve better investment outcomes compared to smaller investors, who are.<sup>10</sup>  
26 This observation suggests that institutional investors benefit from scale and  
27 expertise, which enables them to navigate complex investment landscapes more  
28 effectively. On the other hand, smaller investors need to rely more heavily on  
29 outside classification schemes such as ratings as a means of simplifying and  
30 justifying a decision-making process. The tools presented here, if used properly,  
31 provide valuable insights into investment performance and help smaller  
32 investors make informed decisions. On the one hand, dependence on outside  
33 ratings exacerbates the issue of responsibility-transfer from the plan sponsor to  
34 the consulting firm.<sup>11</sup> On the other, overreliance on statistical systems could lead  
35 to suboptimal outcomes, especially if the underlying metrics are not sufficiently  
36 robust. We propose some robust estimation methods, in this paper.

37 For example, k-means clustering as used in portfolio analysis, identifies a  
38 set of requirements in investment and portfolio construction that are critical in  
39 the present financial landscape, which is highly quantitative, wherein portfolios  
40 are categorized based on various quantitative factors. As financial markets have  
41 become more complex, data-driven approaches to decision-making have long  
42 been considered critical to success. The trend towards utilizing machine learning

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<sup>9</sup>Gennaioli, N., Shleifer A, and Vishny, R., 2015. *Money Doctors*.

<sup>10</sup>Goyal, A. and Wahal, S., 2008. *Selection and Termination of Investment Management Firms by Plan Sponsors*.

<sup>11</sup>Xanthopoulos, A., 2019. *Investment Advising: Pay-to-Play, or Capture?*

1 algorithms, and specifically clustering algorithms such as k-Means and  
 2 classification techniques such as Linear Discriminant Analysis (LDA), has taken  
 3 hold (Hastie, et al., 2025). These are powerful methods that can assist in  
 4 discovering hidden patterns in financial data and in supporting predictive  
 5 modeling and optimizing investment strategies.<sup>12</sup> The method of k-means  
 6 clustering combined with LDA has been studied in numerous domains, from  
 7 finance to risk management and performance assessment (Roberts, et al. 2009).  
 8 K-means clustering, an unsupervised learning technique, divides data into  
 9 separate groups based on common characteristics. It can be effectively employed  
 10 for grouping investment portfolio terms of risk-adjusted returns, beta  
 11 coefficients to market indices, and other relevant performance measures. In  
 12 contrast, LDA is a supervised classification method that sorts financial strategies  
 13 through key attributes, enabling predictions of potential outperformance in  
 14 varying market circumstances.<sup>13</sup> Thus, combining the aforementioned methods  
 15 of k-Means and LDA aid in creating a systematic methodology for assessing  
 16 feedback on financial strategies, optimizing portfolio selection, and performance  
 17 relative to peers in the same asset class.<sup>14</sup> Therefore, the methodologies are  
 18 employed in finance, performance measurement, manager selection, and  
 19 clustering of average-performing strategies. They are used in exploring  
 20 empirical research that shows model effectiveness, identifying key findings, and  
 21 proposing future research avenues. K-Means clustering and LDA for  
 22 performance evaluation enable investment professionals to better understand  
 23 their decision-making processes and establish more advanced techniques for  
 24 managing investment portfolios.<sup>15</sup> We subdivide the ways that these techniques  
 25 have been used in general portfolio performance evaluation, below.

26 Linear Discriminant Analysis (LDA) is a classification technique that  
 27 differentiates between groups based on their attributes (Hastie et al., 2009).  
 28 When integrated with k-means clustering, LDA scores provide a comprehensive  
 29 framework for ranking investment strategies (Brown, et al., 2020). Studies have  
 30 demonstrated that LDA models effectively classify portfolio managers into  
 31 performance categories by utilizing key financial indicators such as alpha, beta,  
 32 and IR (Alzamil, et al., 2021). By leveraging discriminant function scores,  
 33 investment analysts refine decision-making processes and enhance the predictive  
 34 power of financial models.<sup>16</sup>

35 Cornell (2018) investigates combining clustering with LDA in evaluating  
 36 portfolios. The result is dividing financial strategies into several higher  
 37 aggregated clusters, which offer lower complexity based on performance

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<sup>12</sup>Cornell, B., S. Cornell, and A. Cornell, 2018. *The Conceptual Foundations of Investing: A Short Book of Need-to-Know Essentials*.

<sup>13</sup>Brown, T. B., et al., 2020. *Language Models are Few-Shot Learners*.

<sup>14</sup>Gray, P., and Johnson, J., 2011. *The relationship between asset growth and the cross-section of stock returns*.

<sup>15</sup>Renjith, S., Sreekumar, A. and Jathavedan, M., 2021. *A Comparative Analysis of Clustering Quality Based on Internal Validation Indices for Dimensionally Reduced Social Media Data in Advances*.

<sup>16</sup>Lossio-Ventura, J. A., Gonzales, S., Morzan, J., Alatrística-Salas, H., Hernandez-Boussard, T. and Bian, J., *Evaluation of clustering and topic modeling methods over health-related tweets and emails*.

1 measures (Roberts, et al., 2009). Evaluation of performance based on these  
2 clustering techniques can provide insights into financial data as strategies with  
3 similar features are grouped, and corresponding outliers are identified High-  
4 performing clusters have been found to have shared common risk factors like  
5 tracking error and persistent alpha generation. (Alzamil, et al. 2021). Clusters  
6 with high LDA scores have been shown to have higher average returns over the  
7 long run than lower-rated clusters (Brown, et al., 2020). In this study we combine  
8 clustering techniques, with LDA-based classifications.

9 Clusters with moderate performance, in conjunction with LDA scores offer  
10 insight into exposure-based investment strategies providing modest returns  
11 (Alzamil, et al., 2021). Research in this area has concentrated on showcasing as  
12 well as portraying the typical intensity of group execution and investment  
13 choices (Cornell, et al., 2018). In this work we employ clustering and LDA  
14 techniques, to assess the efficacy of ratings assigned by Morningstar, on some  
15 fixed income portfolio strategies. The actual selection of strategies is relied upon  
16 by the institutional investor.

17 In conclusion, this literature review highlights the delicate balance between  
18 relying on objective performance metrics and the careful application of outside  
19 classification schemes, such as ratings. While concerns over advisor conflicts of  
20 interest and the potential risk of rating systems remain, this study demonstrates  
21 that innovative tools in statistical learning can provide significant advantages in  
22 selecting active managers. Unfortunately, the study also points to the fact that  
23 the ratings obtained by at least one investment advisor may mislead. By  
24 uncovering patterns in data that traditional methods overlook, statistical learning  
25 has the potential to reshape the investment landscape, offering investors more  
26 accurate and timely insights into strategy performance. Rating schemes, when  
27 applied transparently and in conjunction with advanced analytical techniques,  
28 can enhance decision-making and contribute to better institutional investor  
29 performance outcomes.

## 30 31 32 **Methodology**

33  
34 Admissible investment strategies employed in retirement plans,  
35 endowments, and foundations, specifically focus on “long-only” investments but  
36 still fall within three key asset categories: fixed income, equity, and hedge funds.  
37 We focus on actual long-only fixed income strategies currently available for  
38 investment. The categories of fixed income are further subdivided into universes,  
39 such as Aggregate Bonds, Corporate Bonds, Emerging Market Bonds, etc. This  
40 methodology outlines the data collection, performance evaluation, and comparison  
41 of actual portfolio outperformance to the ratings assigned by Morningstar on these  
42 same portfolio strategies. The primary data source for this analysis was Yahoo  
43 Finance, where the Net Asset Value (NAV) and monthly returns for a variety of  
44 investment strategies were obtained, for the period of October 2018 to  
45 September 2023. Yahoo Finance offers a wide array of publicly available  
46 financial data, which makes it an ideal resource for this study. Additionally,

1 performance and risk ratings provided by Morningstar, available through Yahoo  
2 Finance, were integrated into the dataset to help evaluate the relative  
3 effectiveness of the investment strategies. These ratings offer insights into how  
4 each strategy performs relative to its peers, based on opinions and contact with  
5 the manager by consultant/advisors.

6 The first step in the methodology involved filtering the dataset to select  
7 investment strategies based on predefined criteria within General Corporate  
8 Bond, which is a universe in fixed income portfolios. This process ensured that  
9 only those strategies with complete data were included in the analysis, while  
10 strategies with missing data or discrepancies were excluded or cleaned before  
11 further processing. Using Excel, the dataset was filtered to focus specifically on  
12 strategies that had data for at least the last 24 months, as this time frame allows  
13 for more stable and reliable analysis. The goal was to ensure that all strategies  
14 selected for analysis were comparable in terms of data completeness and  
15 relevance.

16 The second step is study involved employing a rolling regression approach  
17 to measure the performance of selected strategies over time. Specifically, 24-  
18 month rolling windows of data were used for 36 strategies within the “Aggregate  
19 Bond” universe. The key steps were:

20 Rolling Regression to Benchmark: Each strategy’s returns were regressed  
21 against eight preselected indices to measure the relationship between the  
22 strategy’s performance and the benchmark. The selected indices comprised the  
23 Bloomberg Global Aggregate Bond and seven ICE/BofA Corporate Bond Total  
24 Return indices that span the whole corporate credit curve (AAA, AA, A, BBB,  
25 BB, B, CCC).<sup>17</sup> The regression output provided insights into the degree of  
26 correlation between the strategy and the benchmark, and the resulting beta  
27 coefficients were used as independent variables to explain risk adjusted  
28 performance (Information Ratio, IR). The 24-month rolling returns for the  
29 selected 36 strategies were regressed against the benchmark indices. These  
30 regressions formed the foundation for understanding how each strategy  
31 performed in comparison to its benchmark. The results allowed for a better  
32 understanding of which strategies generated consistent alpha over time and how  
33 they responded to changes in market conditions.

34 Rolling Information Ratio (IR): The Information Ratio (IR) for each strategy  
35 was calculated to assess risk-adjusted performance. The IR was derived by  
36 subtracting the benchmark returns from the strategy's returns and dividing the  
37 difference by the tracking error (standard deviation of active returns). This  
38 metric was used to gauge how much value each manager was adding above the  
39 benchmark, adjusting for risk. By regressing the IR values of all strategies  
40 against the betas obtained as above, the study identified strategies that  
41 consistently outperformed their benchmarks versus those that were prone to  
42 underperformance, given their risk levels.

43 Regression of Information Ratio (IR): To explore the relationship between  
44 market exposure and risk-adjusted performance, the IR values were regressed  
45 against the strategy’s beta coefficients. Beta measures the sensitivity of the



1 strategy's returns to overall market movements. This regression was designed to  
2 evaluate how much market exposure contributed to overall risk-adjusted returns  
3 and to see whether active management added value beyond market movements.  
4 The IR values were analyzed by regressing them against the beta coefficients of  
5 each strategy. This step assesses the credit levels of market exposure which  
6 affected active returns. The process is repeated four times, for Information Ratio  
7 of the Current Month, of six months forward, twelve months forward and two  
8 years forward. An Autoregressive-level 1 model is used for this process.

9 The third step involved producing reports, in the form of data on betas and  
10 IR. Statistical methods of linear regression, linear discriminant analysis (LDA),  
11 and k-means clustering were applied to data on reports produced. Regressing IR  
12 against betas of credit exposure provided the contribution to IR generated by  
13 such exposure. After that, the regression model was augmented with dummy  
14 variables, each capturing one of the five-star ratings assigned by Morningstar.  
15 The results were further analyzed using LDA and k-means clustering.  
16 Specifically, LDA classified the strategies in the sample into "invest" or "not  
17 invest" by finding a discriminant score that quantified these two categories based  
18 on their beta coefficients. By using these techniques, we were able to identify  
19 issues with the efficacy of the ratings assigned to investment strategies. Our  
20 study could be extended into future directions, such as exploring logistic  
21 regression models to analyze the relationship between strategy performance and  
22 analyst ratings. Discriminant Analysis could also be applied to create a score that  
23 predicts which strategies are most likely to outperform in the future.  
24 Additionally, more advanced machine learning models, including regime-  
25 switching. For the purposes of this study, we performed the following steps using  
26 Excel's functions.

27 Preparing the Data in Reports: The first step involved reviewing the dataset  
28 in 'Reports' to ensure consistency and to check for missing data. Additional  
29 columns were added to help locate the word "Rating" in the description of selected  
30 portfolios and extracting the rating next to that word. The =FIND("rating",  
31 [Cell]) function was used to locate "Rating" within the description. To handle  
32 missing instances, we used: =IFERROR(FIND("rating", [Cell]), "No Rating  
33 Found").

34 The function =MID([Cell], [Position of Rating] + 7, 1) was used to extract the  
35 rating number that follows the word "rating:." The "+7" skips the word "rating"  
36 and the colon. IFERROR was again applied to avoid errors, returning "N/A" if  
37 no rating was found. The TRIM function was used to remove extra spaces,  
38 ensuring that rating values were consistent. The extracted ratings were then  
39 converted into numeric values using the VALUE function, which flagged invalid  
40 entries.

41 Creating Dummy Variables: Dummy variables transform categorical data  
42 into numerical form so that it can be used in statistical models. For example, to  
43 convert "Genre" (e.g., Action, Drama, Comedy) into numeric, for each category,  
44 a "Yes/No" variable is created:

- 45 • For "Action," the dummy variable is 1 if the genre is Action and 0

- 1 otherwise.
- 2 • For "Drama," the dummy variable is 1 if the genre is Drama and 0
- 3 otherwise.
- 4 • For "Comedy," the dummy variable is 1 if the genre is Comedy and 0
- 5 otherwise.
- 6

7 By using dummy variables, we captured the effect of each category on the

8 variable being studied (e.g., ratings). Dummy Variables were created for each

9 possible rating value (e.g., 1, 2, 3). For each column, an IF formula was used to

10 check whether the extracted rating matched a particular number. For a one-star

11 rating by Morningstar: =IF([Rating]=1, 1, 0), etc. Once dummy variables were

12 created, unnecessary columns were removed. A check was carried out to ensure

13 the data was clean and all ratings were correctly extracted and matched to the

14 descriptions. In Excel, the Data Analysis Tool was used to perform all

15 regressions. The Y Range (dependent variable, IR) and X Range (beta

16 coefficients to indices and dummy variables for ratings) were selected. The

17 "Labels" option was ticked. Other necessary options like residuals were checked.

18 The table below shows part of the data for IR predicted at time 0 (current) against

19 betas and dummy variables.

20

21 **Table 1. Current Month Information Ratio against Betas to Indices and Rating**

22 **[0,1] Variables**

Portfolios that are 'General Corporate Bond'	alpha	1 Bloomberg	11 ICE BofA	15 ICE BofA	20 ICE BofA	8 ICE BofA	10 ICE BofA	12 ICE BofA	5 ICE BofA	1	2	3	4	Curr Mo
JPMorgan Strategic Income Opportunities Fund - RS (JSOR)	0.001	-0.040	-0.237	0.131	0.067	0.216	-0.164	0.143	0.020	-	-	-	1.00	0.659
JPMorgan Strategic Income Opportunities Fund - Select (JS)	0.001	-0.035	-0.202	0.067	0.004	0.282	-0.143	0.124	0.017	-	-	1.00	-	0.624
JPMorgan Strategic Income Opportunities Fund - A (JSOAX)	0.000	-0.054	-0.199	0.057	0.044	0.262	-0.142	0.125	0.021	-	-	1.00	-	0.462
Dunham Floating Rate Bond Fund - A (DAFRX), Universe:G	0.001	-0.174	-0.371	-0.126	0.686	0.215	-0.587	0.735	0.146	-	-	1.00	-	0.284
Dunham Floating Rate Bond Fund - C (DCFRX), Universe:G	0.000	-0.132	-0.432	-0.111	0.796	0.140	-0.609	0.764	0.141	-	1.00	-	-	0.211
Manning & Napier Fund Inc - Core Plus Bond Series Fund -	0.003	0.311	-1.850	2.497	0.756	-0.880	-0.098	0.025	0.121	-	-	-	1.00	0.196
JPMorgan Strategic Income Opportunities Fund - C (JSOCX)	0.000	-0.060	-0.219	0.070	0.098	0.229	-0.143	0.131	0.019	-	-	1.00	-	0.177
Western Asset SMASH Series C Fund - C (LMLCX), Univers	-0.001	-0.318	0.949	-2.503	0.492	1.434	0.297	0.326	-0.094	-	-	-	-	0.038
Columbia Income Opportunities Fund - Y (CIOYX), Univers	0.000	0.024	-0.604	0.719	1.039	-0.912	0.187	0.652	0.083	-	-	1.00	-	0.025
Columbia Income Opportunities Fund - RS (CEPRX), Univer	0.000	0.026	-0.522	0.668	0.876	-0.819	0.205	0.656	0.068	-	-	1.00	-	0.012
Columbia Income Opportunities Fund - R4 (CPPRX), Univer	0.000	0.017	-0.611	0.723	1.059	-0.926	0.194	0.657	0.081	-	-	1.00	-	0.008

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## Linear Regression with Dummy Variables

It can be argued that the use of data analytics techniques was promulgated by (i) the availability of methods by statistical analysts, and/or (ii) pressures from regulators regarding the access to legal avenues by the institution investor through the Department of Labor's Fiduciary Rule. What is the simplest statistical model that an organization with fiduciary responsibility can implement, to address the efficacy of advice in the form of portfolio strategy ratings, based on the variables created through a process that follows the Methodology above? The equation is given below:

$$IR(p, t + j) = b_0 + \sum_{i=1}^8 b_{i,j} \beta_{i,p} + \sum_{r=1}^4 d_{i,j} \mathbb{I}_{[r],p} + \varepsilon \quad (1)$$

where:  $IR(p, t + j)$  = estimated information ratio  $j$  months ahead,  $j = 0, 6, 12, 23$  months.

1  $b_{i,j}$  = regression coefficient of  $IR(p, t + j)$  against beta for index  $i = 1, 2,$   
2  $3, \dots, 8.$

3  $\beta_{i,p}$  = estimated beta of portfolio  $p$ 's IR against index  $i$ (Rolling  
4 Regression to Benchmark)

5  $d_{i,j}$  = regression coefficient of  $IR(p, t + j)$  against rating-r-indicator  
6 variable  $\mathbb{I}_{[r],p}$ .

7  $\mathbb{I}_{[r],p}$  = indicator variable for Morningstar rating  $r =$  one, two, three or  
8 four stars.

9  
10 For example, the first investment strategy in Table 1 above has the label:  
11  $p =$  JPMorgan Strategic Income Opportunities Fund - R5 (JSORX), Universe:  
12 General Corporate Bond, Rating:4 Stars Low, Unconstrained: N, IsoRisk:0.12,  
13 Count:59

14 Equation (1) would apply to JPMorgan Strategic Income Opportunities Fund as  
15 follows:

$$\begin{aligned}
 & IR(JPMorgan, t + 0) \\
 & = b_0 + b_{1,0}(-0.040) + b_{2,0}(-0.237) + b_{3,0}(0.131) \\
 & + b_{4,0}(0.067) + b_{5,0}(0.216) + b_{6,0}(-0.164) + b_{7,0}(0.143) \\
 & + b_{8,0}(0.020) + \\
 & + d_{1,0}(0) + d_{2,0}(0) + d_{3,0}(0) + d_{4,0}(1) + \varepsilon \\
 & (2)
 \end{aligned}$$

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24 The tables below show the coefficients and  $p$ -values of the twelve variables in  
25 equation (1):

26  
27 **Table 2. Regression Coefficients of IR against Betas and Rating-Dummy Variables**

	$j =$ Current Month	$j =$ Six Months Forward	$j =$ Twelve Months Forward	$j =$ Twenty Four Months Forward
	Coefficients	Coefficients	Coefficients	Coefficients
Intercept	0.432	0.566	0.322	-4.762
Bloomberg Global Aggregate Bond (LEGATRUU)	-0.052	-0.325	-1.286	-1.555
ICE BofA AAA US Corporate Index (BAMLCC0A1AAATRIV)	<b>-0.813</b>	<b>-1.111</b>	<b>-1.957</b>	<b>3.079</b>
ICE BofA AA US Corporate Index (BAMLCC0A2AATRIV)	<b>-1.075</b>	<b>-1.332</b>	<b>-1.668</b>	<b>4.590</b>
ICE BofA Single-A US Corporate Index (BAMLCC0A3ATRIV)	<b>-0.504</b>	<b>-0.560</b>	<b>-0.911</b>	<b>5.756</b>
ICE BofA BBB US Corporate Index (BAMLCC0A4BBBTRIV)	<b>-1.297</b>	<b>-1.652</b>	<b>-1.380</b>	<b>6.608</b>
ICE BofA BB US High Yield Index (BAMLHYH0A1BBTRIV)	<b>-1.232</b>	<b>-1.972</b>	<b>-2.130</b>	<b>4.783</b>
ICE BofA Single-B US High Yield Index (BAMLHYH0A2BTRIV)	<b>-0.607</b>	<b>-0.649</b>	-0.782	9.016
ICE BofA CCC & Lower US High Yield Index (BAMLHYH0A3CMTRIV)	<b>-3.940</b>	<b>-6.265</b>	<b>-8.350</b>	<b>-6.175</b>
Morningstar Rating = One Star, $d_1$	<b>1.713</b>	<b>2.257</b>	2.673	-1.826
Morningstar Rating = Two Stars, $d_2$	0.094	-0.134	<b>0.883</b>	<b>-2.094</b>
Morningstar Rating = Three Stars, $d_3$	0.201	0.091	0.748	-1.802
Morningstar Rating = Four Stars, $d_4$	<b>0.347</b>	0.282	0.718	-1.580

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1 **Table 3. Statistical Significance of Coefficients of IR against Betas and Dummy**  
 2 **Variables**

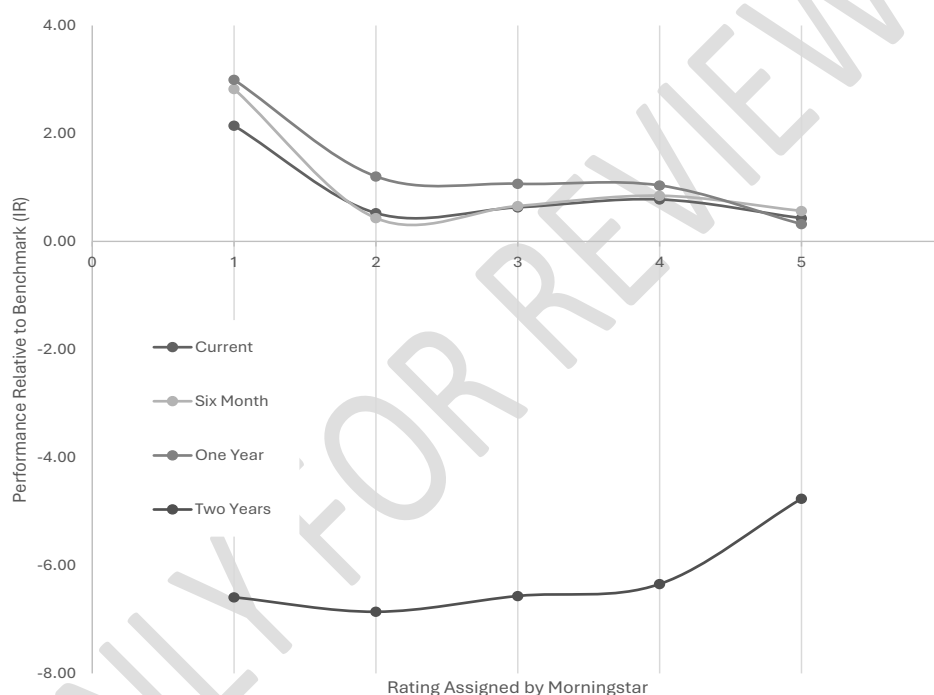
	<i>j</i> = Current Month	<i>j</i> = Six Months Forward	<i>j</i> = Twelve Months Forward	<i>j</i> = Twenty Four Months Forward
	<i>P</i> -value	<i>P</i> -value	<i>P</i> -value	<i>P</i> -value
Intercept	0.055	0.050	0.595	0.595
Bloomberg Global Aggregate Bond (LEGATRUU)	0.823	0.280	0.056	0.056
ICE BofA AAA US Corporate Index (BAMLCC0A1AAATRIV)	<b>0.008</b>	<b>0.005</b>	<b>0.020</b>	<b>0.020</b>
ICE BofA AA US Corporate Index (BAMLCC0A2AATRIV)	<b>0.000</b>	<b>0.000</b>	<b>0.028</b>	<b>0.028</b>
ICE BofA Single-A US Corporate Index (BAMLCC0A3ATRIV)	<b>0.007</b>	<b>0.018</b>	<b>0.070</b>	<b>0.070</b>
ICE BofA BBB US Corporate Index (BAMLCC0A4BBBTRIV)	<b>0.000</b>	<b>0.000</b>	<b>0.087</b>	<b>0.087</b>
ICE BofA BB US High Yield Index (BAMLHYH0A1BBTRIV)	<b>0.000</b>	<b>0.000</b>	<b>0.002</b>	<b>0.002</b>
ICE BofA Single-B US High Yield Index (BAMLHYH0A2BTRIV)	<b>0.016</b>	<b>0.041</b>	0.244	0.244
ICE BofA CCC & Lower US High Yield Index (BAMLHYH0A3CMTRIV)	<b>0.001</b>	<b>0.000</b>	<b>0.008</b>	<b>0.008</b>
Morningstar Rating = One Star, $d_1$	<b>0.008</b>	<b>0.006</b>	0.117	0.117
Morningstar Rating = Two Stars, $d_2$	0.541	0.497	<b>0.047</b>	<b>0.047</b>
Morningstar Rating = Three Stars, $d_3$	0.190	0.636	0.084	0.084
Morningstar Rating = Four Stars, $d_4$	<b>0.021</b>	0.130	0.079	0.079

### 6 Ratings and Outperformance are Inversely Related

7  
 8 The reader might have expected that the dummy variable coefficients in  
 9 Table 2 above would be ranked in magnitude as  $d_1 < d_2 < d_3 < d_4$ . In other words,  
 10 the dummy variable  $\mathbb{I}_{[r=4],p}$  that is for strategies rated as four-stars, would add  
 11 to the Information Ratio more than what dummy variable  $\mathbb{I}_{[r=3],p}$  did, which  
 12 would add more than  $\mathbb{I}_{[r=2],p}$ , which would add more than  $\mathbb{I}_{[r=1],p}$  did. But, that  
 13 does not happen here, which poses doubt on the efficaciousness of this rating  
 14 system. The diagram below shows that the best alternative available to the  
 15 institutional investor, with access to such portfolio ratings, is the group rated the  
 16 lowest, by at least this investment consultant. There is a pronounced negative  
 17 relation between ratings and the addition to IR of each rating, for  $j = 0, 6$  and 12  
 18 months. This relationship might be of concern to institutional investors, although  
 19 an outright breach of fiduciary responsibility cannot and should not be concluded  
 20 based on this data. The reasons are that (i) there is often a lag between the time  
 21 an analyst/consultant looks at the materials related to due diligence of a strategy,  
 22 for the purpose of assigning a rating, and (ii) in the time it takes for a rating to  
 23 be assigned, a strategy rated high may underperform due to just the change in  
 24 the business cycle. For example, an Inflation-Linked strategy may have exposure  
 25 to short-duration credit yields while anticipating inflationary episodes, in  
 26 contrast to a ‘pure play’ in this universe, and thus be rated four stars. By the time  
 27 such a rating is entered, short-term yields may collapse, resulting in  
 28 underperformance. Thus, ratings and outperformance may appear to have an  
 29 inverse relation, contrary to common sense. The vertical axis in Figure 1 below  
 30 shows the intercept plus addition to Information Ratio (IR or Relative  
 31 Performance, risk adjusted) for each of the ratings one-, two-, three- and four-  
 32 stars (the rating of five-stars is incorporated into the intercept as standard  
 33 dummy-variable estimation requires). For example, the intercept  $b_0$  plus the  
 34 addition to current month IR attributed to rating one-star is  $0.432 + 1.713 =$   
 35  $2.145$ . The same figures for 6-month and 12-month IR are  $0.556 + 2.257 = 2.824$   
 36 and  $0.322 + 2.693 = 2.995$ , shown as starting points of the lines in the top panel

1 of Figure 1, which pertains to IR for current, a six-month, and twelve-month  
 2 forward projection. From that point as we move forward to ratings 2 (two-star),  
 3 3 (three-star) and 4 (four-star), information ratio declines, not because the  
 4 intercept  $b_0$  changes, but because the contribution to IR from each rating  
 5 declines. For an allocation horizon of zero, six, and twelve months forward,  
 6 the institutional investor should have invested the funds managed into portfolio  
 7 strategies that are rated the lowest, by Morningstar. That may cause worry, not  
 8 necessarily from the perspective of intentional breach of fiduciary duty, but as  
 9 stemming from time inefficiencies or other hidden biases faced by the  
 10 advisor/consultant assigning the rating. As mentioned above, the precise reasons  
 11 for the patterns found is beyond the scope of this study.

12  
 13 **Figure 1.** *Addition to Relative Performance by Rating, Current and Projected*



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### 15 **Investment Managers Produce Negative ‘alpha’ Two Years Hence**

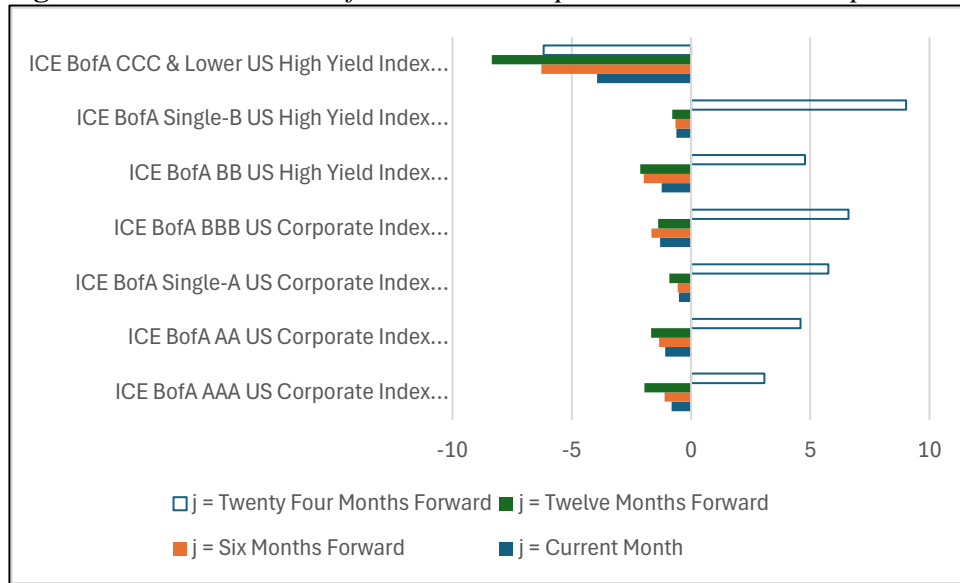
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17 A business cycle in the U.S. may last two years, and investment strategies  
 18 that worked at the start will underperform if not pivoted on time. The  
 19 autoregressive model that we use captures this non-pivoted relation of IR against  
 20 beta coefficients and the rating-dummy variables. The bottom panel of Figure 1  
 21 shows that, if strategy betas to indices remain the same, IR in two years will be  
 22 around the -6.5 or less region (a healthy information ratio should range around  
 23 positive 2.0 and above). It may be the case that consulting firms often claim that  
 24 their ratings represent outperformance through the whole business cycle, and/or  
 25 for two years into the future. Given the fact that, based on our estimates a strategy  
 26 that has not pivoted in time will underperform in two years, might such claims  
 27 be less than accurate, if not properly tested statistically? The bottom panel of

1 Figure 1, shows that, given the already negative  $b_0 = -4.762$  that applies across  
 2 all ratings, performance two years hence for one-, two-, three-, and four-star  
 3 ratings is -6.589, -6.857, -6.564 and -6.343, respectively, if strategies did not  
 4 change their allocation schemes by that time. One would have to presume that  
 5 the due diligence process engaged in by Morningstar evaluates future pivoting,  
 6 and/or portfolio managers voluntarily disclose such plans and then follow them  
 7 exactly. The only conclusion one can discern from the results is that ratings and  
 8 outperformance align only two years into the future, with the four-star rating  
 9 managing to subtract the least ( $b_0 - 1.580$ ) from information ratio, for strategies  
 10 that have not pivoted. Unless consultants gauge and rigorously evaluate such  
 11 plans by the portfolio manager, any potential claims hypotheses that their ratings  
 12 do not represent performance two years into the future, might be hard to properly  
 13 reject.

14 The statistically significant coefficients for the seven ICE BofA indices  
 15 from Table 2, above, show that the credit curve captured by these indices  
 16 subtracts from performance for zero, six, and twelve months forth, and adds to  
 17 performance for two years forward, apart from CCC exposure, assuming no  
 18 pivoting of strategy before the presumed change in the business cycle. This part  
 19 makes the relation of ratings to performance more complicated. It seems that,  
 20 without pivoting, the markets will carry performance in the absence of still ( $b_0$ )  
 21 and with no carry from ratings.

22  
 23 ICE BofA AAA US Corporate Index (BAMLCC0A1AAATRIV)  
 24 ICE BofA AA US Corporate Index (BAMLCC0A2AATRIV)  
 25 ICE BofA Single-A US Corporate Index (BAMLCC0A3ATRIV)  
 26 ICE BofA BBB US Corporate Index (BAMLCC0A4BBBTRIV)  
 27 ICE BofA BB US High Yield Index (BAMLHYH0A1BBTRIV)  
 28 ICE BofA Single-B US High Yield Index (BAMLHYH0A2BTRIV)  
 29 ICE BofA CCC & Lower US High Yield Index  
 30 (BAMLHYH0A3CMTRIV)  
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1 **Figure 2.** Addition to IR Performance and Exposure to the Credit Corporate Curve

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## 6 **The Relation between Information Ratio and Recommendation Based on**

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The ratings comprise categorical data and thus are hard to compare to quantitative performance; unless ratings were changed to a quantitative score, achieved through linear discriminant analysis (LDA). The goal of ratings is to help the institutional client reach some binary decision of ‘invest’ or ‘not invest’ upon looking at them, in its simplest form. We make an arbitrary but not so far-fetched assumption that the representative plan sponsor of an institutional account will consider investment portfolios rated four-stars and above, as candidates. For all of the four ‘forward-looking’ versions of our IR model (zero, six, twelve and two years) we follow the steps below in devising the linear discriminant score, which is now quantitative.<sup>18</sup> According to Fisher (1936), the linear discriminant score is  $X_p = \sum_{i=1}^8 \lambda_i \beta_{i,p}$  with  $\beta_{i,p}$  the same as in (1).

- a) We separated the strategies into one group rated four-stars and above (and thus it has portfolios that are recommended to the institutional client), and one below four-star (and thus not recommended) by Morningstar. We found the average for each of the indices. For example, for IR in the current month, the average beta coefficients for recommended and not recommended strategies were as shown below:

<sup>18</sup>This methodology exactly replicates the original work by Fisher 1936. *The Use of Multiple Measurements in Taxonomic Problems*.

Bloomberg Global Aggregate Bond (LEGATRUU)	ICE BofA AAA US Corporate Index (BAMLCC0A1A AATRIV)	ICE BofA AA US Corporate Index (BAMLCC0A2A ATRIV)	ICE BofA Single-A US Corporate Index (BAMLCC0A3A TRIV)	ICE BofA BBB US Corporate Index (BAMLCC0A4B BBTRIV)	ICE BofA BB US High Yield Index (BAMLHYH0A1 BBTRIV)	ICE BofA Single-B US High Yield Index (BAMLHYH0A2 BTRIV)	ICE BofA CCC & Lower US High Yield Index (BAMLHYH0A3 CMTRIV)
-0.266	-0.696	0.486	1.546	-0.371	0.158	-0.129	0.137
-0.088	-0.561	0.624	0.940	-0.305	0.072	0.163	0.095

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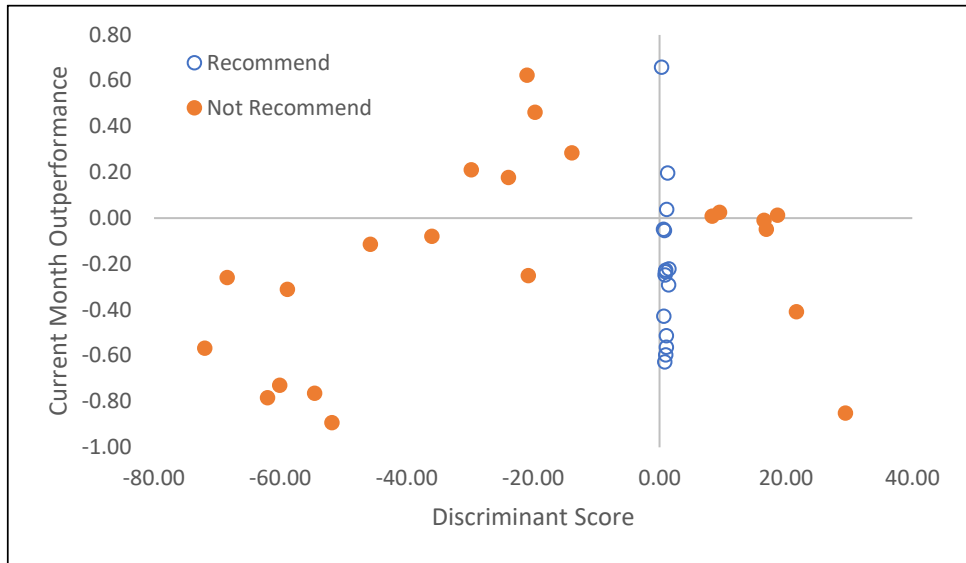
- b) For each beta coefficient to an index, we found the square of differences  $d_i$  of the means, weighted by  $\lambda_i$ , between recommended and not recommended:  $D^2 = \{\sum_{i=1}^8 \lambda_i \beta_{i,p}\}^2$
- c) For the  $\beta_{i,p}$  coefficients of the strategies recommended, we found their difference from their individual means,  $[\beta_{1,p} - \overline{\beta_{1,p}}, \beta_{2,p} - \overline{\beta_{2,p}}, \dots, \beta_{8,p} - \overline{\beta_{8,p}}]$  for each portfolio,  $p$ . We multiplied that vector by its transpose to get the terms of the covariance matrix,  $S_{pq}^2$ .
- d) We pre-multiplied and post-multiplied  $S_{pq}^2$  by vector  $\lambda_i$ , to get  $S^2 = \sum_{p=1}^8 \sum_{q=1}^8 \lambda_p \lambda_q S_{pq}$ .
- e) To arrive at  $X_p$ , we used solver.xls in Excel to maximize the ratio  $D^2/S^2$  with respect to the ‘weights’ of the discriminant score,  $\lambda_i$ . The resulting discriminant function score was:

$$X_p = \sum_{i=1}^8 \lambda_i \beta_{i,p} = 1.00\beta_{1,p} - 1.89\beta_{2,p} - 0.87\beta_{3,p} + 0.83\beta_{4,p} + 0.40\beta_{5,p} - 0.68\beta_{6,p} - 0.85\beta_{7,p} - 5.94\beta_{8,p}$$

The average score of the strategies recommended based on a Morningstar score of four-star and above was 0.95, and that for strategies not recommended was -23.53. But their standard deviations were 0.31 and 33.08, respectively. Why was the standard deviation of strategies not recommended, so wide? These score values did not change between the IR models (zero, six, twelve and two years) because they were based only on the beta coefficients, which were the same for all four versions. Changing the star categories to a recommendation score allowed for a comparison between quantified recommendation and IR performance, in zero, six, twelve and two years, shown in the two diagrams below (the diagrams for six- and twelve-months forward were like current month and are thus not shown). We observe in figure 3 that the strategies not recommended fall very wide to the right and the left of those recommended. In other words, there are investment strategies to the right of the 0.95 score which have an exceedingly high recommendation score and would thus have received a four- or five-star by Morningstar; but which perform dismally. Two years forward, that dismal performance of highly recommended strategies disappears. We would have expected a continuous positive relation between discriminant score and IR. That does not happen anywhere. Further analysis with more data is needed here to discern the patterns of mismatch between IR and the discriminant function score that implies recommendation for investment based on ratings. This mismatch may not lead to the conclusion that fiduciary responsibility is denigrated.

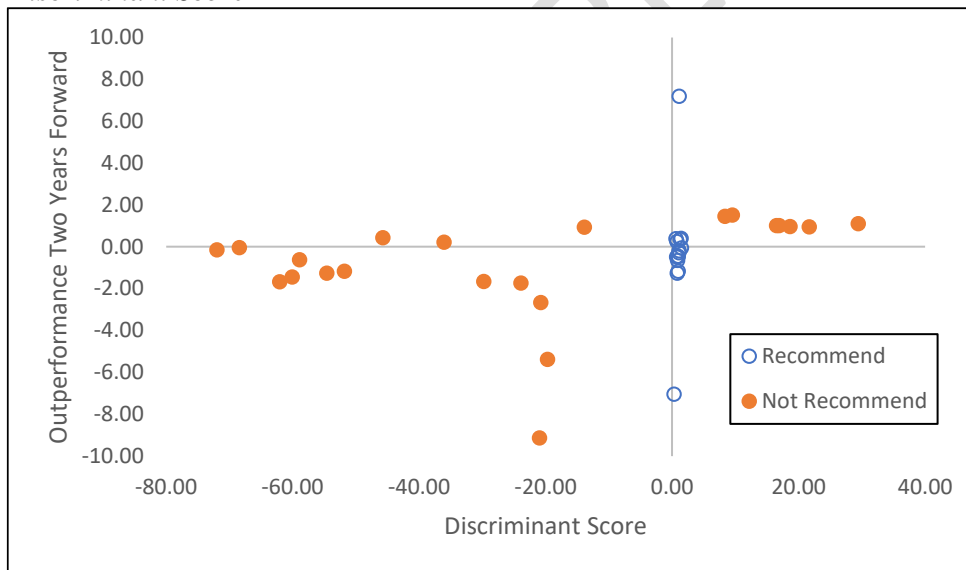


1 **Figure 3.** *Information Ratio for the Current Month against Recommendation*  
 2 *Discriminant Score*



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5 **Figure 4.** *Information Ratio for Two Years Forward against Recommendation*  
 6 *Discriminant Score*



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10 **Clusters show a Vague Relation between Ratings and Performance**

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 12 Does the discriminant score of recommendation based on ratings bear any  
 13 semblance to average performance over current month, and six-, twelve month  
 14 and to years forward? We ran a k-means clustering algorithm in RStudio, with  
 15 five clusters (since Morningstar has five-star ratings) of all four measures of  
 16 performance (current, six months, twelve months, two years). We wanted to see  
 17 if the four measures of IR performance would somehow group by themselves,  
 18 into unsupervised clusters that would align with an average discriminant score

1 for recommendation. The results in Table 4, below, were optimistic but with  
 2 great variation. Based on risk-adjusted fund performance (IR), cluster one, for  
 3 example, shows a recommendation score that vary widely from -62.06 to 0.96  
 4 with an average of -19.54 and average performance over four periods of -0.91.  
 5 The same numbers for the second cluster are -5.66 and 0.00; for the next cluster  
 6 -36.17 and -0.58, etc. Figure 5 shows that there may be a positive relation  
 7 between ratings and performance, albeit a very vague one. The average  
 8 discriminant function score in a cluster of four-period performance weakly  
 9 aligns with the average performance across strategies and periods in the same  
 10 cluster. The linear relation has an R-Square of only 41.07% which is high given  
 11 the degrees of freedom. Unfortunately, the range of Recommend scores in each  
 12 cluster are too wide to justify a level of confidence that the recommendations  
 13 resulting from Morningstar ratings and the risk-adjusted performance across  
 14 time have a fund-by-fund correspondence that the institutional investor could  
 15 semi-blindly rely on. In clusters 1 and 2, which contain most portfolios, we  
 16 would expect ratings to be such that the Recommend score gravitated around -  
 17 19.54 and -5.66, respectively.

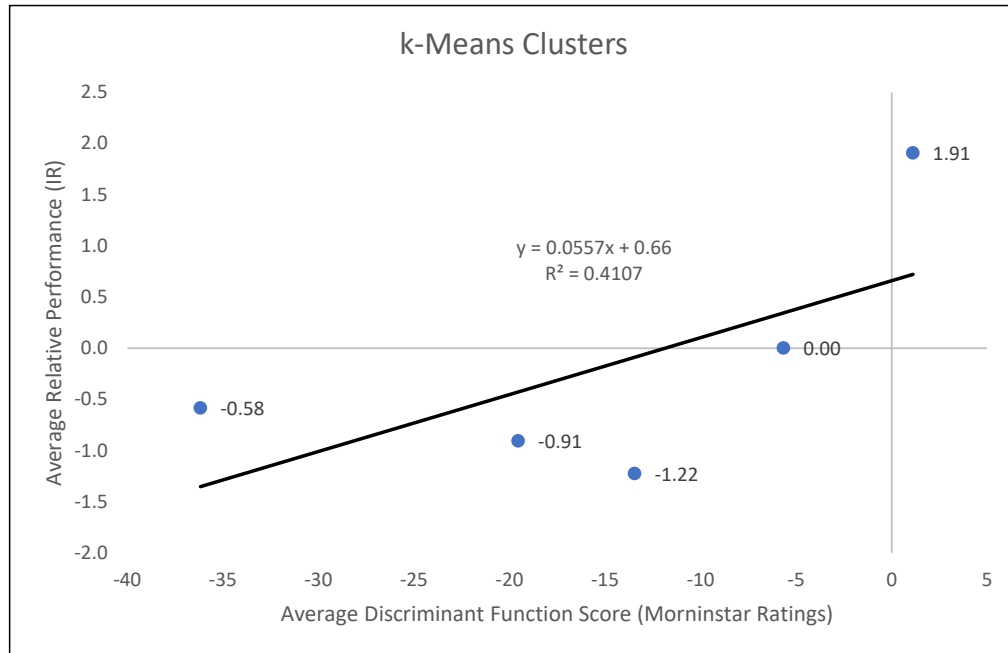
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**Table 4. Clusters of Performance in Four Periods and Corresponding Recommendation Scores**

Portfolio	Cluster	Recommend	Curr Mo	6 Mo(s) Fwd	12 Mo(s) Fwd	23 Mo(s) Fwd	Average
AllianceBernstein Corporate Income Shares (ACISX), Rating:4 star, Above Average	1	-62.06	-0.78	-1.33	-2.25	-1.67	
BNY Mellon Corporate Bond Fund - Investor (BYMIX), Rating:5 star, Below Average	1	-60.10	-0.73	-1.23	-1.49	-1.45	
BNY Mellon Corporate Bond Fund - M (BYMMX), Rating:5 star, Below Average	1	-58.90	-0.31	-0.69	-0.79	-0.62	
Columbia Corporate Income Fund - R4 (CIFRX), Rating:4 star, Above Average	1	0.68	-0.43	-0.34	-1.96	-0.48	
Columbia Corporate Income Fund - R5 (CPIRX), Rating:4 star, Above Average	1	0.82	-0.63	-1.16	-2.19	-1.26	
Columbia Corporate Income Fund - Y (CRIYX), Rating:4 star, Above Average	1	0.84	-0.25	-0.64	-0.74	-0.65	
Invesco Corporate Bond Fund - A (ACCBX), Rating:4 star, Above Average	1	0.92	-0.23	-0.59	-0.52	-0.49	
Invesco Corporate Bond Fund - R5 (ACCWX), Rating:5 star, Above Average	1	0.95	-0.23	-0.60	-0.61	-0.46	
JPMorgan Corporate Bond Fund - R6 (CBFVX), Rating:4 star, Above Average	1	0.96	-0.60	-1.12	-1.90	-1.16	
	Cluster 1	-19.54	-0.47	-0.85	-1.38	-0.92	-0.91
JPMorgan Corporate Bond Fund - Select (CBFSX), Rating:4 star, Above Average	2	-71.99	-0.57	-0.69	-0.25	-0.15	
JPMorgan Strategic Income Opportunities Fund - R5 (JSORX), Rating:4 Star	2	-68.43	-0.26	-0.61	-0.48	-0.04	
MainStay Indexed Bond Fund - A (MIXAX), Rating:4 stars above average,	2	-45.75	-0.11	-0.18	-0.28	0.43	
MainStay Indexed Bond Fund - I (MIXIX), Rating:4 stars above average,	2	-36.05	-0.08	-0.13	-0.24	0.21	
Manning & Napier Fund Inc - Core Plus Bond Series Fund - I (MNCPX), Rating:4	2	-13.90	0.28	0.44	1.00	0.94	
Western Asset SMASH Series C Fund - C (LMLCX), Rating:5 stars high, Iso	2	0.61	-0.05	-0.09	-0.25	0.38	
American Funds Corporate Bond Fund - 529C (COBCX), Rating:2 star, Below	2	0.75	-0.06	-0.15	-0.28	0.24	
Columbia Corporate Income Fund - A (LIAX), Rating:3 stars above average	2	1.05	-0.51	-0.67	-0.25	-0.29	
Columbia Corporate Income Fund - C (CIOCX), Rating:2 star, Above Average	2	1.09	-0.56	-0.69	-0.27	-0.20	
Columbia Income Opportunities Fund - R (CIORX), Rating:2 star, Above Average	2	1.25	0.20	0.27	0.04	0.36	
Columbia Income Opportunities Fund - R4 (CPPRX), Rating:3 star, Above Average	2	1.43	-0.29	-0.17	-0.22	0.40	
Columbia Income Opportunities Fund - R5 (CEPRX), Rating:3 star, Above Average	2	1.45	-0.22	-0.09	-0.51	-0.06	
Columbia Income Opportunities Fund - Y (CIOYX), Rating:3 star, Above Average	2	8.33	0.01	-0.08	-0.23	1.45	
Columbia Income Opportunities Fund - Z (CIOZX), Rating:3 star, Above Average	2	9.51	0.03	-0.09	-0.25	1.52	
Dunham Floating Rate Bond Fund - A (DAFRX), Rating:3 star, Above Average	2	16.52	-0.01	-0.08	-0.21	1.01	
Dunham Floating Rate Bond Fund - C (DCFRX), Rating:2 star, Above Average	2	16.90	-0.05	-0.09	-0.21	1.00	
Invesco Corporate Bond Fund - C (ACCX), Rating:2 star, Above Average	2	18.64	0.01	-0.03	-0.21	0.96	
Invesco Corporate Bond Fund - R (ACCZX), Rating:3 star, Above Average	2	21.66	-0.41	-0.38	0.34	0.95	
JPMorgan Corporate Bond Fund - A (CBRAX), Rating:3 star, Above Average, Iso	2	29.41	-0.16	-0.23	-0.22	0.43	
	Cluster 2	-5.66	-0.15	-0.19	-0.16	0.50	0.00
JPMorgan Corporate Bond Fund - C (CBRCX), Rating:2 star, Above Average, Iso	3	-54.58	-0.76	-1.42	0.13	-1.26	
JPMorgan Strategic Income Opportunities Fund - A (JSOAX), Rating:3 Star	3	-51.83	-0.89	-1.47	0.09	-1.17	
JPMorgan Strategic Income Opportunities Fund - C (JSOCX), Rating:3 Star	3	-29.81	0.21	0.13	1.21	-1.65	
JPMorgan Strategic Income Opportunities Fund - Select (JSOSX), Rating:3	3	-23.90	0.18	0.16	0.26	-1.73	
MainStay Indexed Bond Fund - INV (MIXNX), Rating:3 stars above average	3	-20.75	-0.25	-0.41	-0.35	-2.67	
	Cluster 3	-36.17	-0.30	-0.60	0.27	-1.70	-0.58
Western Asset Corporate Bond Fund - C (LWBOX), Rating:2 stars high, Iso	4	1.12	0.04	0.11	0.30	7.18	1.91
Western Asset Corporate Bond Fund - P (LCBPX), Rating:2 Stars High, Iso	5	-20.97	0.62	0.69	1.02	-9.13	
Western Asset SMASH Series EC Fund - EC (LMECX), Rating:1 star high, Iso	5	-19.69	0.46	0.44	1.01	-5.38	
Western Asset SMASH Series M Fund - M (LMSMX), Rating:2 stars high, Iso	5	0.31	0.66	0.63	1.32	-7.04	
	Cluster 5	-13.45	0.58	0.59	1.12	-7.18	-1.22

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1 **Figure 5.** Clusters-averages: Performance in Four Periods and Recommendation  
 2 Score



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## Conclusion

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8 In this study, we investigate the role of investment advising and portfolio  
 9 recommendations made by consulting firms such as Morningstar to institutional  
 10 clients. A key concern in the context of U.S. regulatory bodies is the issue of  
 11 breach of fiduciary duty, where advisers encourage portfolio managers to offer  
 12 monetary benefits in exchange for favorable ratings of their investment  
 13 strategies. Although we did not find any robust correspondence between ratings  
 14 and relative performance, we would be hard-pressed to conclude that  
 15 Morningstar, or any other investment advisor for that matter, is abrogating  
 16 fiduciary responsibility. Having said that, we examined a list of statistical models  
 17 that could be used as quality control methodologies of rating efficacy.

18 Investment advising/consulting firms play a central role in determining the  
 19 allocation of retiree funds into investment strategies. In this study, generally  
 20 accepted metrics in active management help assess the efficacy of information  
 21 produced by Morningstar, in its role as portfolio evaluator and issuer of one-to-  
 22 five-star ratings. We use the betas against eight indices representing the credit  
 23 yield curve, as the x-variables and regress them against IR. Portfolio managers  
 24 decide to buy and sell assets at the various parts of the yield curve. The assigned  
 25 ratings should not deviate materially from the active outperformance generated  
 26 here as Information Ratio (IR). Quantitative methods allow institutional  
 27 investors to systematically classify strategies based on performance irrespective  
 28 of the ratings assigned to strategies. Finance implements clustering algorithms  
 29 such as k-Means and classification techniques like Linear Discriminant Analysis  
 30 (LDA) as approaches for identifying hidden patterns in optimal investment

1 portfolio selection. Using such methods we find that investment performance of  
2 strategies rated, and the ratings themselves, do not align. For example, the  
3 regression dummy variable for the least favorable Morningstar rating adds the  
4 most to the risk-adjusted outperformance (Information Ratio, IR), leading to the  
5 easy, ‘arbitrage’ process of simply allocating retiree funds to the lowest-rated  
6 portfolios. Discriminant function scores, on the other hand, span all over the  
7 performance range for both recommended and not recommended strategies.  
8 Several highly recommended strategies based on Morningstar ratings would  
9 produce dismal risk-adjusted performance. For the five clusters identified based  
10 on outperformance of the current month, six-months forward, 12-months  
11 forward and two years forward, combined, risk-adjusted performance is  
12 positively related to the linear discriminant score of recommendation based on  
13 ratings in very general terms; obscuring the other negative relations between  
14 ratings and outperformance obtained in other methods. The results of this study  
15 may be of interest in the regulatory arena of fiduciary responsibility, a full legal  
16 analysis of which is out-of-scope for this study.

17 Ratings and outperformance inversely relate because of the business cycle or  
18 an assessment-to-rating time gap and are not necessarily due to intentional breach  
19 of fiduciary duty. Ratings mildly align with risk-adjusted outperformance two years  
20 forward, but that is not enough for consultants to claim that their rating process is  
21 ‘forward looking’ as investment managers consistently produce negative alpha two  
22 years hence, irrespective of rating. The relation between consultant ratings and risk-  
23 adjusted performance of rated strategies is obscure. Recommended strategies for  
24 investment, at the very least, fail to exhibit performance that is higher than strategies  
25 not recommended. Highly recommended strategies exhibit significant  
26 underperformance across all kinds of time intervals. There appears to be only an  
27 imprecise, vague positive relation between clusters of performance and ratings. Still,  
28 our analysis cannot suggest that the issue of pay-to-play appears to manifest  
29 significantly in the ratings provided by investment consultants like Morningstar.  
30 The methods of k-means clustering and LDA isolated patterns of disconnect  
31 between ratings and relative outperformance, in this application of finance.  
32 Further study is required in this area, to precisely pinpoint the areas where  
33 investment consultants who assign ratings miss it as far as the future  
34 outperformance of strategies rated exceedingly high is concerned. The  
35 institutional investor cannot rely solely on ratings to select investment strategies  
36 in which the beneficiaries’ funds can be allocated. The use of statistical models  
37 will augment that process if appropriately used.

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